

The BOLD Response

Douglas C. Noll

Department of Biomedical Engineering

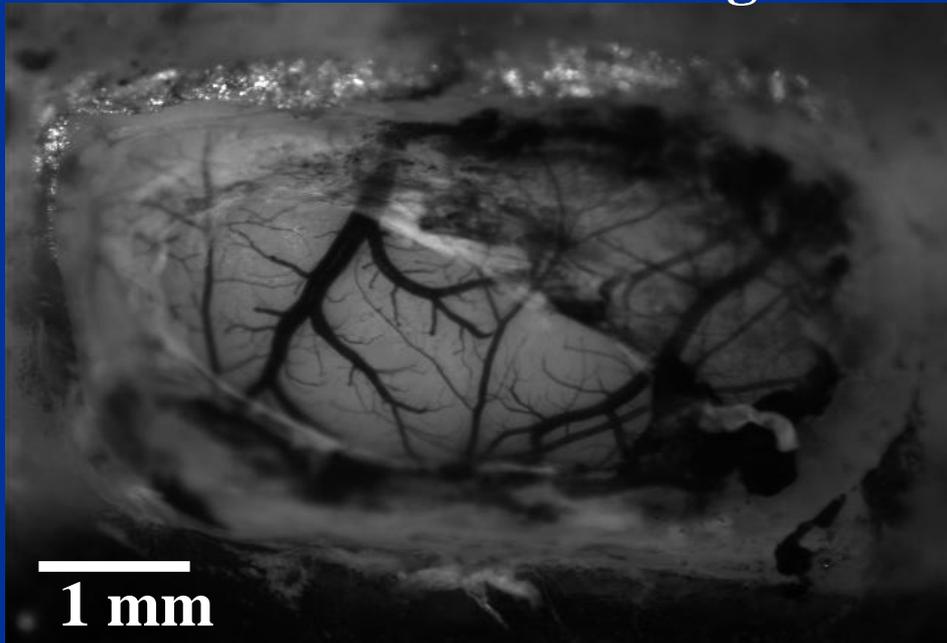
University of Michigan

Outline

- Mechanism of the BOLD response
 - Susceptibility of blood
 - Fick's relationship/mass balance
- Spatial specificity of BOLD and alternatives
- Evidence for and mechanisms of non-linearity
- Implications for fMRI Studies
- Conclusions

Dynamic Vascular Changes

Anatomical Image



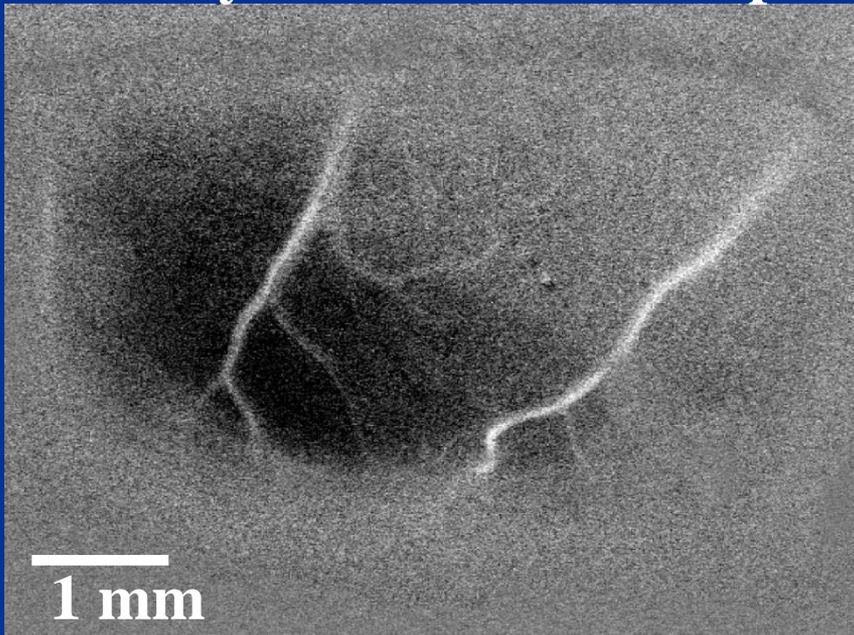
620 nm (BOLD-like)



Optical imaging of intrinsic signal (OIS) from a rat

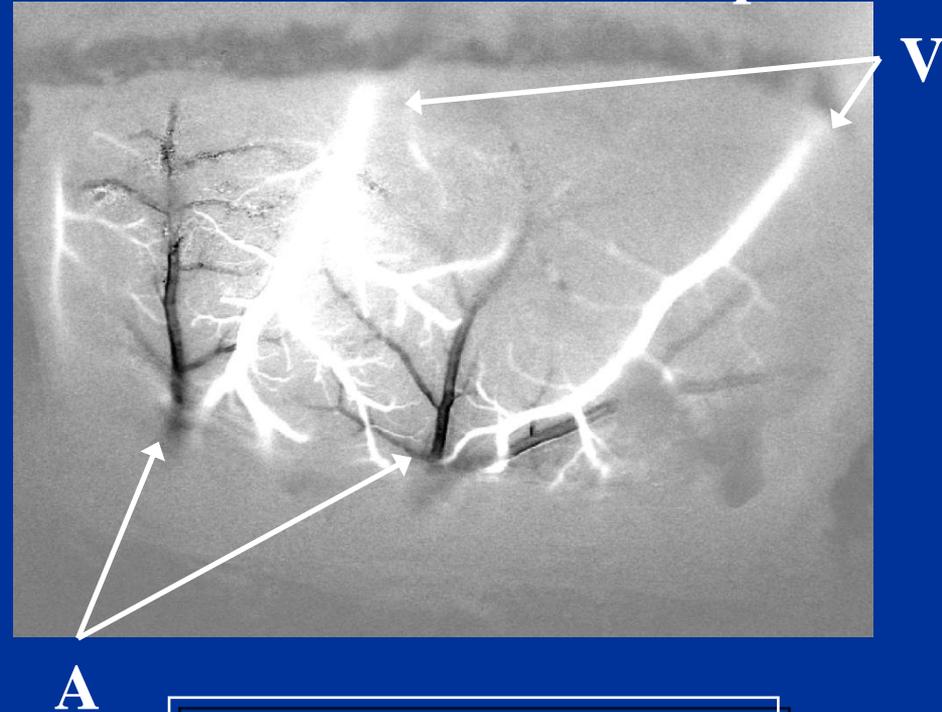
Interesting Temporal Features

Early OIS Decrease Map



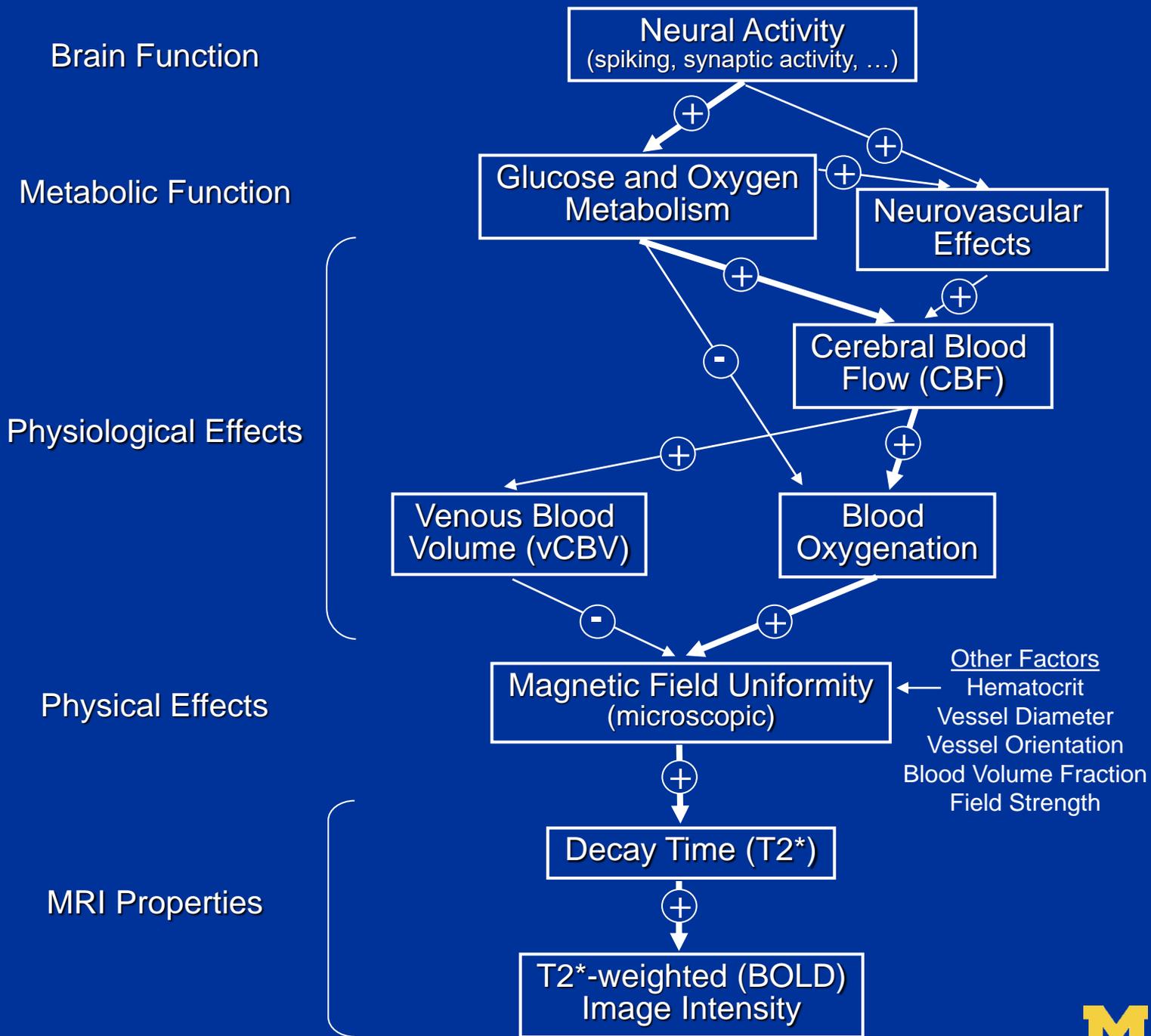
Well-localized temporally and spatially

Late OIS Increase Map



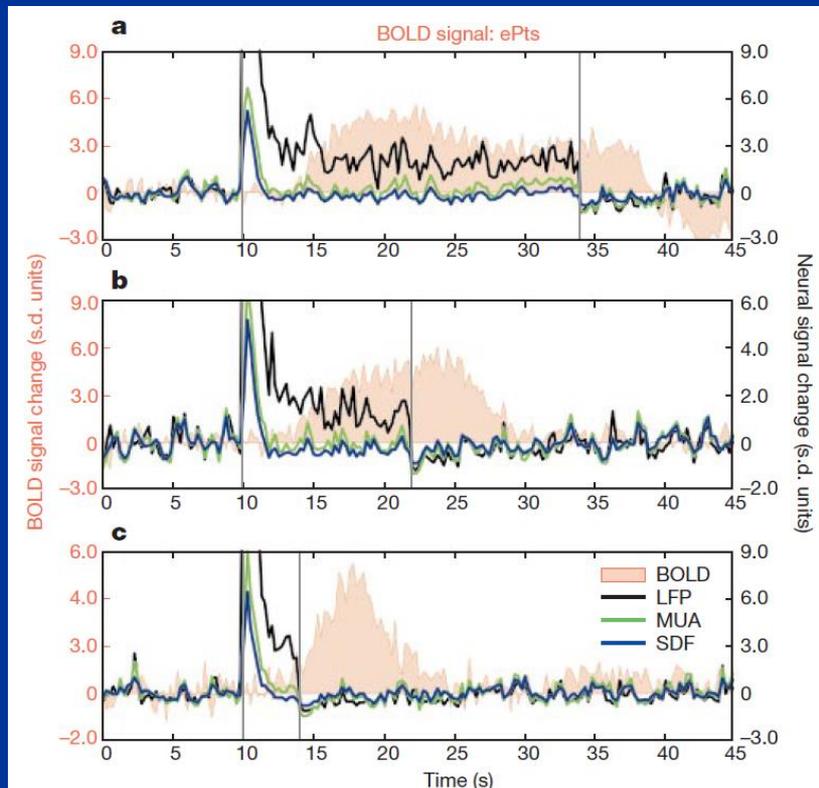
Less well-localized temporally and spatially, but larger response

The BOLD Effect



What Part of Neural Activity does BOLD Represent?

- Spiking or synaptic activity?
 - Post-synaptic recycling of neurotransmitters is the very metabolically intensive

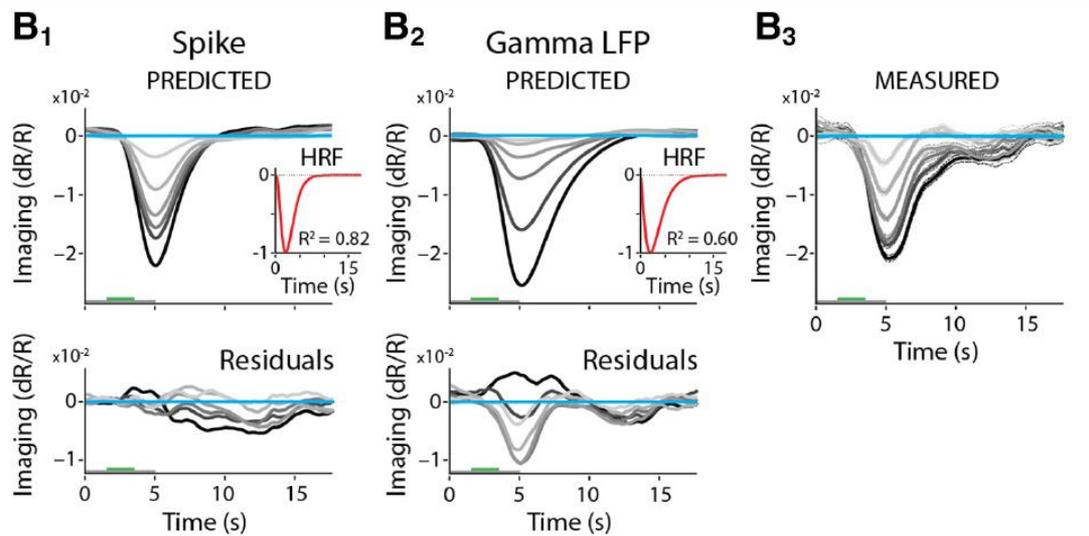


Local field potentials (LFP) correlate more strongly to BOLD than multi-unit activity (MUA)

Synaptic activity > spiking

(Logothetis et al, Nature, 2001)

Spiking or Synaptic Activity?



In this study, spiking correlates with BOLD better than LFP

Spiking > synaptic activity

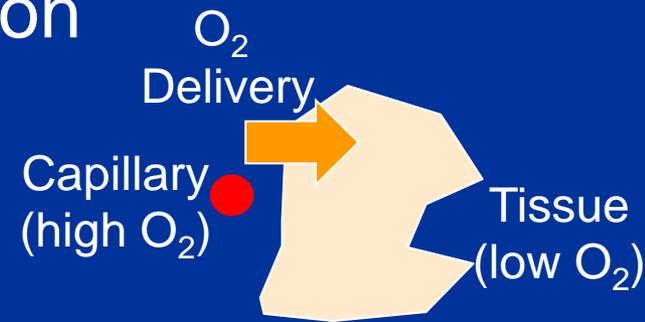
(Lima et al, J Neurosci, 2014)

- Consensus is that BOLD more strongly reflects the input to a neuronal population, rather than only its spiking output to other regions.

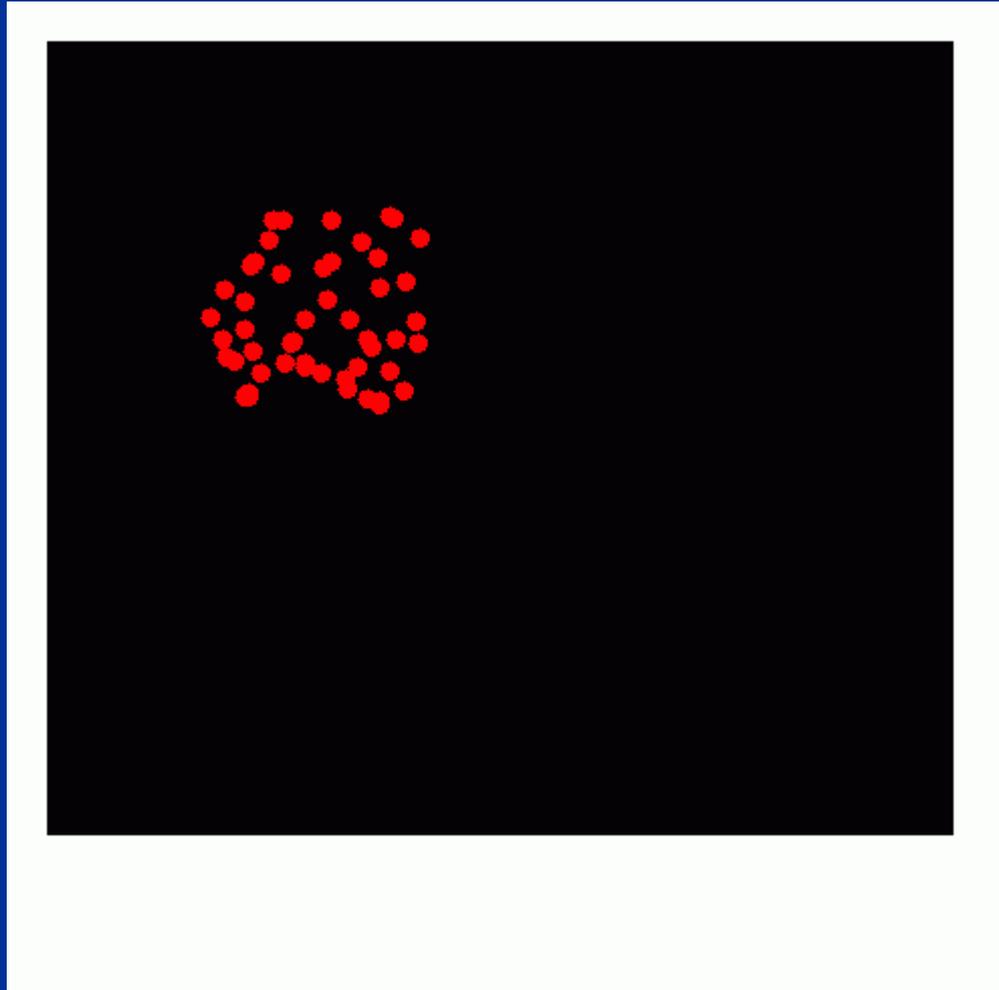
- A number of studies that have found BOLD changes independent of neural firing

What Drives the BOLD Response?

- Evolutionarily speaking:
 - Need for O_2 for increased metabolism
 - Need to take away metabolic products
- Delivery of O_2 is driven by diffusion
 - Rate of delivery depends on concentration gradients
 - Increase delivery by decreasing tissue O_2 (happens with metabolism) and increasing cap O_2 (happens with increased flow)
- Can you deliver more O_2 without flow increases?
 - Yes, but that's not what happens in healthy tissues



Diffusion Delivery of O₂



From: <http://cronodon.com/BioTech/Diffusion.html>

What are the mechanisms of increased flow (CBF)?

- Complicated!
- Blood flows increase through increases in arteriole diameter
- Smooth muscle surrounding arterioles is relaxed by variety of metabolic products

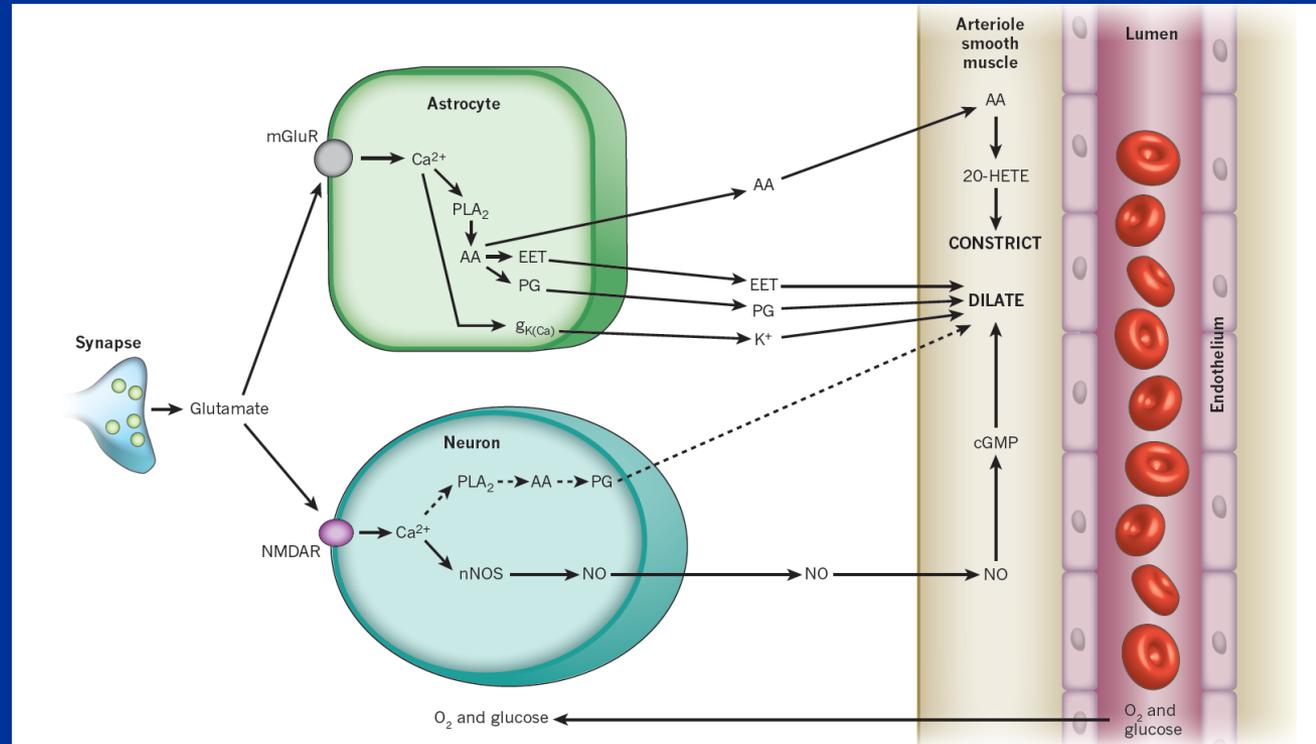


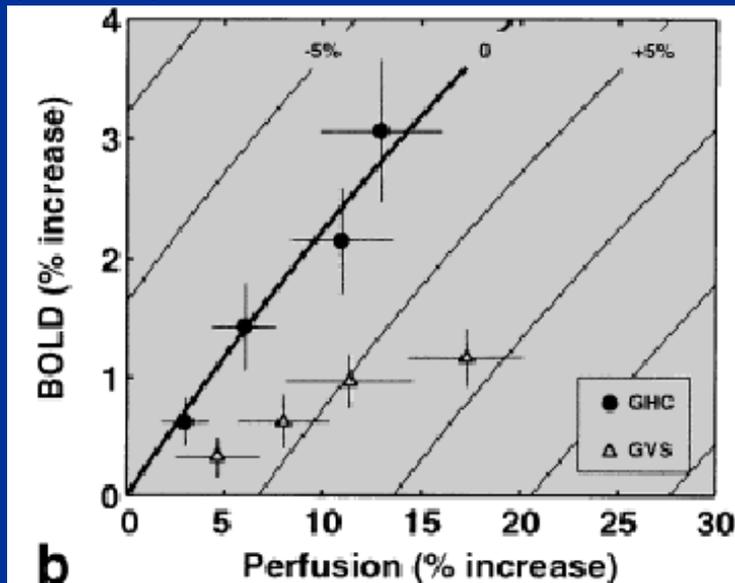
Figure 2 | Major pathways by which glutamate regulates cerebral blood flow. Pathways from astrocytes and neurons (left) that regulate blood flow by sending messengers (arrows) to influence the smooth muscle around the arterioles that supply oxygen and glucose to the cells (right, shown as the vessel lumen surrounded by endothelial cells and smooth muscle). In neurons, synaptically released glutamate acts on *N*-methyl-D-aspartate receptors (NMDAR) to raise $[Ca^{2+}]_i$, causing neuronal nitric oxide synthase (nNOS) to release NO, which activates smooth muscle guanylate cyclase. This generates cGMP to dilate vessels. Raised $[Ca^{2+}]_i$ may also (dashed line)

generate arachidonic acid (AA) from phospholipase A₂ (PLA₂), which is converted by COX2 to prostaglandins (PG) that dilate vessels. Glutamate raises $[Ca^{2+}]_i$ in astrocytes by activating metabotropic glutamate receptors (mGluR), generating arachidonic acid and thus three types of metabolite: prostaglandins (by COX1/3, and COX2 in pathological situations) and EETs (by P450 epoxygenase) in astrocytes, which dilate vessels, and 20-HETE (by ω -hydroxylase) in smooth muscle, which constricts vessels. A rise of $[Ca^{2+}]_i$ in astrocyte endfeet may activate Ca^{2+} -gated K^+ channels ($g_{K(Ca)}$), releasing K^+ , which also dilates vessels.

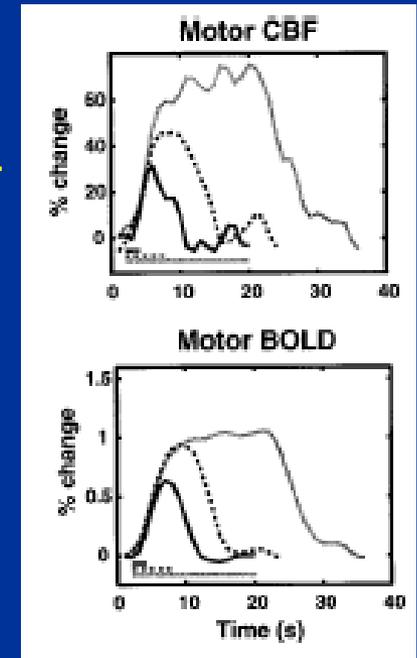
The BOLD Response

- Changes in cerebral blood flow (CBF) drive the BOLD changes
 - Temporal characteristics of the CBF changes dominate the BOLD temporal response

BOLD and CBF changes with graded hypercapnia and visual stimulation



BOLD and CBF changes have similar temporal characteristics



Magnetic Susceptibility of Blood

- The distortion of the magnetic field is:

$$\Delta B = \chi_m B_0$$

- Some relative susceptibility values

Material (relative to water)	χ_m ($\times 10^{-6}$)
Water	0
Room Air	9.4
Pure oxygen gas	11
Deoxygenated Blood (Hct = 1)	2.3

Magnetic Susceptibility of Blood

- An expression for the susceptibility of blood is:

$$\chi_{\text{blood}} = \text{Hct}(Y\chi_{\text{oxy}} + (1-Y)\chi_{\text{deoxy}}) + (1-\text{Hct})\chi_{\text{plasma}}$$

- Hct is hematocrit and
- Y is blood oxygenation

- But, $\chi_{\text{oxy}} = \chi_{\text{plasma}} = \chi_{\text{tissue}} = \chi_{\text{water}} = 0$, so:

$$\chi_{\text{blood}} = \text{Hct}(1-Y)\chi_{\text{deoxy}}$$

- Example

- If Hct = .4 and Y = .7, $\chi_{\text{blood}} = 0.12 \chi_{\text{deoxy}} = 0.28 \times 10^{-6}$

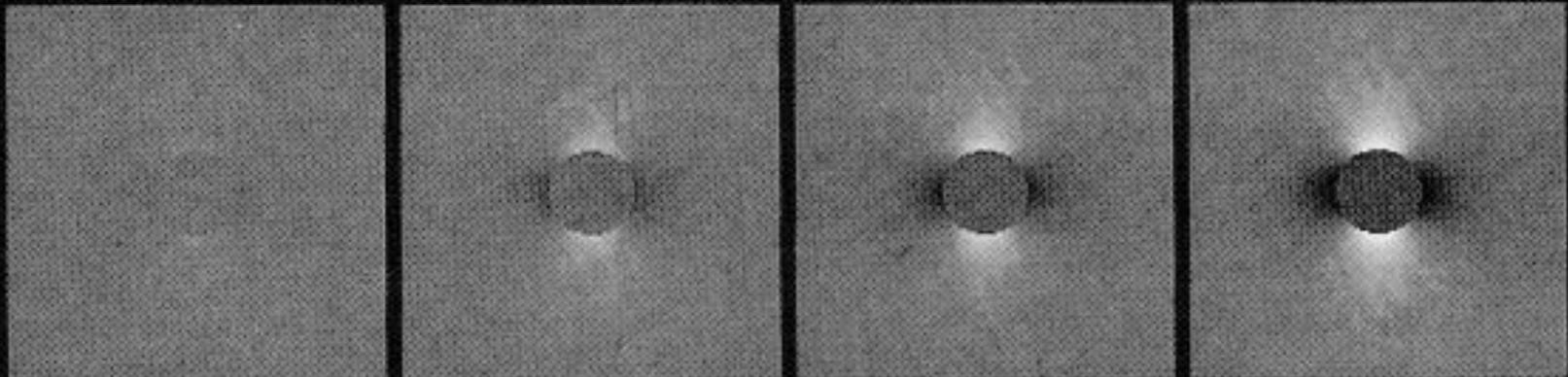
ΔO_2 saturation

90%

60%

30%

0%



± 19.1

± 76.2

± 133.4

± 190.6

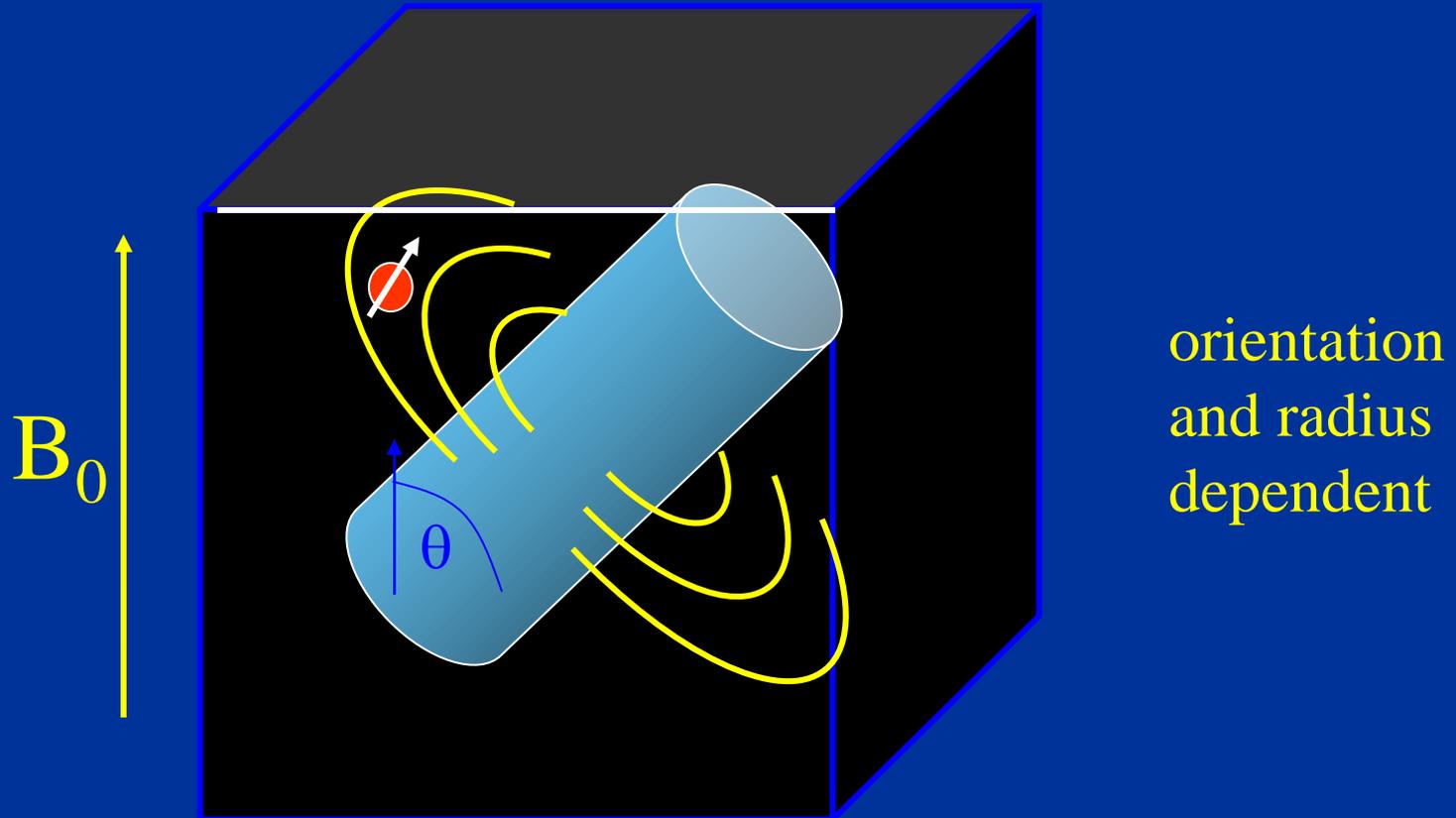
-190.6

190.6

$\Delta\omega$ (rad/sec)

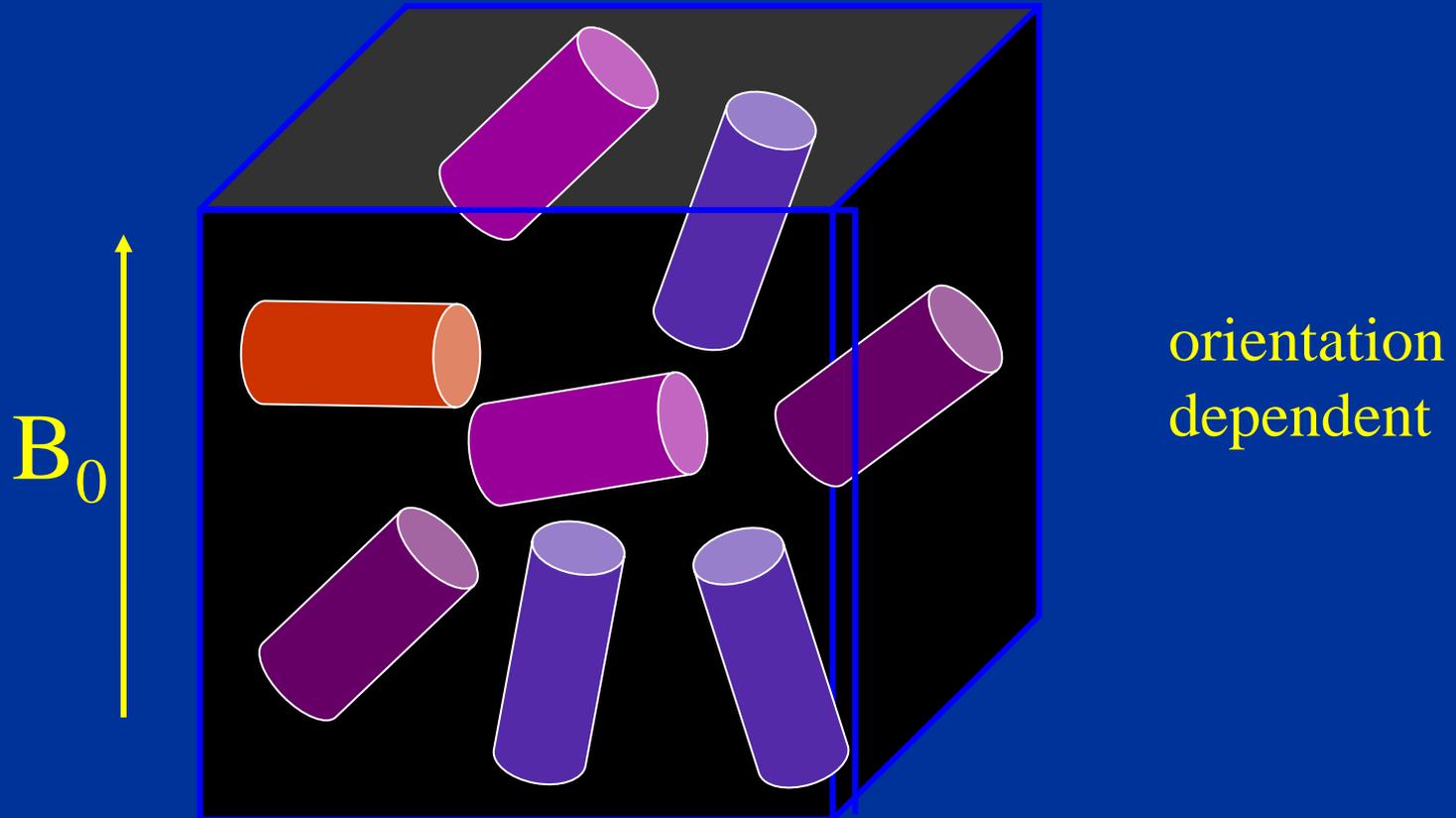
rad = 5 μm
vol = 4%
 $\theta = 90^\circ$
Bo = 1.5 T
D = 1.0 $\mu\text{m}^2 / \text{ms}$

Extravascular Contribution



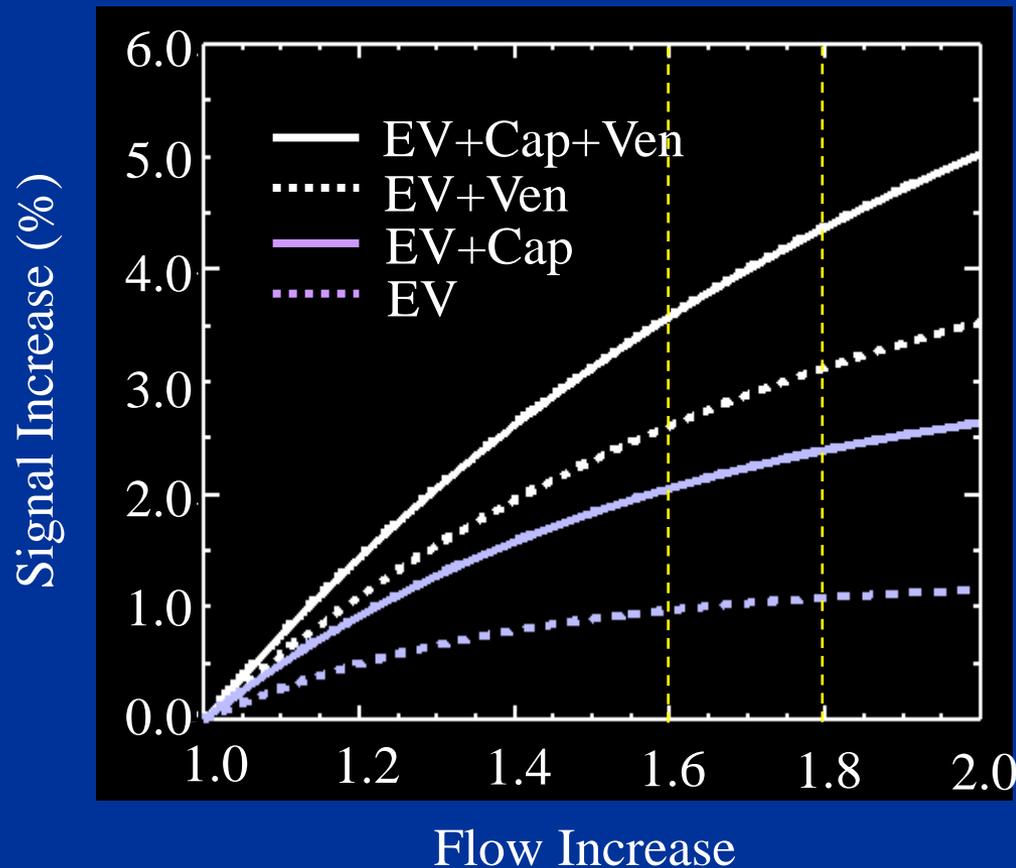
$$\Delta\omega(r, \theta, \phi) = \Delta\omega' \sin^2(\theta) (a/r)^2 \cos(2\phi)$$

Intravascular Contribution: heterogeneous orientation



$$\Delta\omega(\theta) = \Delta\omega' [3\cos^2(\theta) - 1] / 3$$

Tissue and Blood Contributions



field strength
dependence

What is T2*?

- T2* has two parts:
 - Inter-molecular interactions leading to dephasing, a.k.a. T2 decay
 - Macroscopic or mesoscopic static magnetic field inhomogeneity leading to dephasing, a.k.a. T2'

$$\frac{1}{T2^*} = \frac{1}{T2'} + \frac{1}{T2}$$

- Pulse sequence issues:
 - Spin echoes are sensitive to T2
 - Gradient echoes are sensitive to T2*

What is $R2^*$?

- We often talk about “rates” instead of time constants, e.g.:

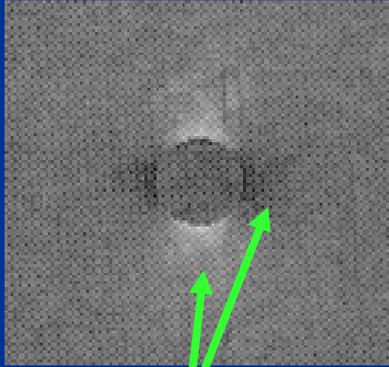
$$R2^* = \frac{1}{T2^*}$$

- So the decay rate is given by the sum of the rates:

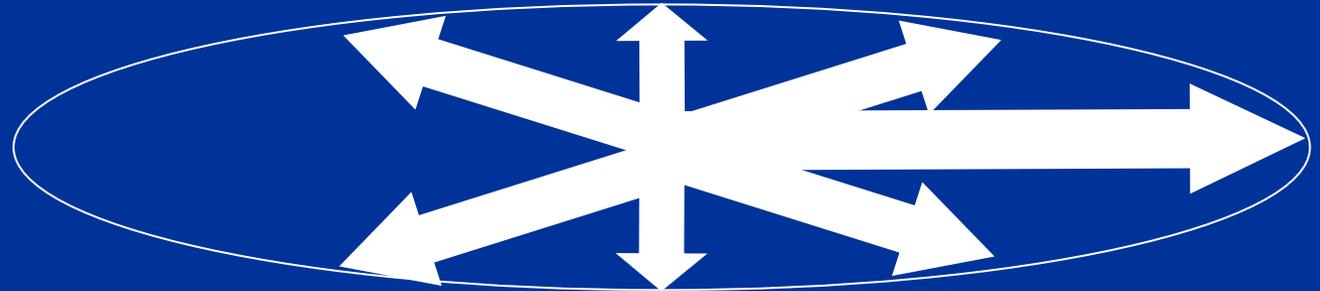
$$R2^* = R2 + R2'$$

Dephasing from Deoxyhemoglobin

60%

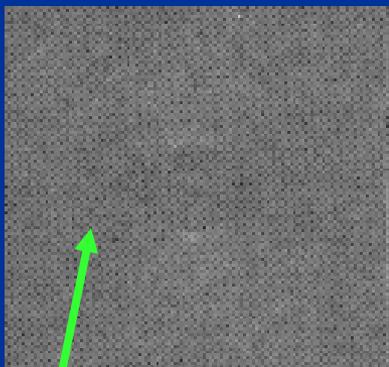


Different Fields

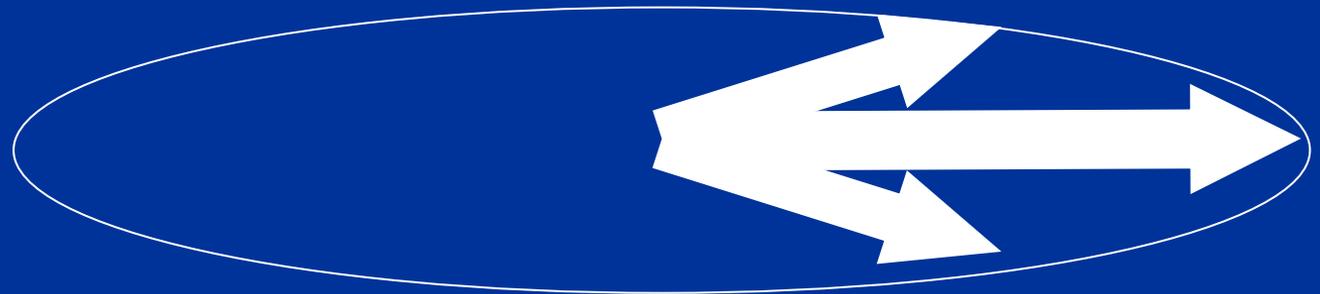


Vs.

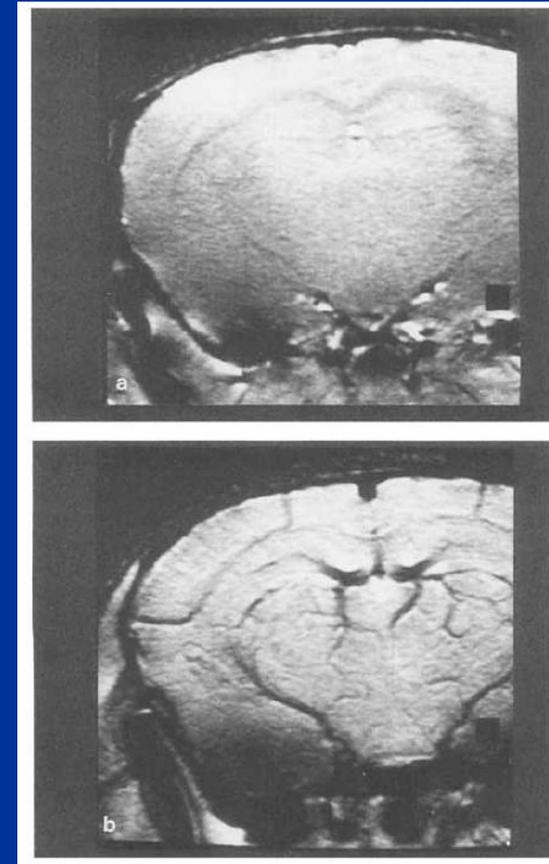
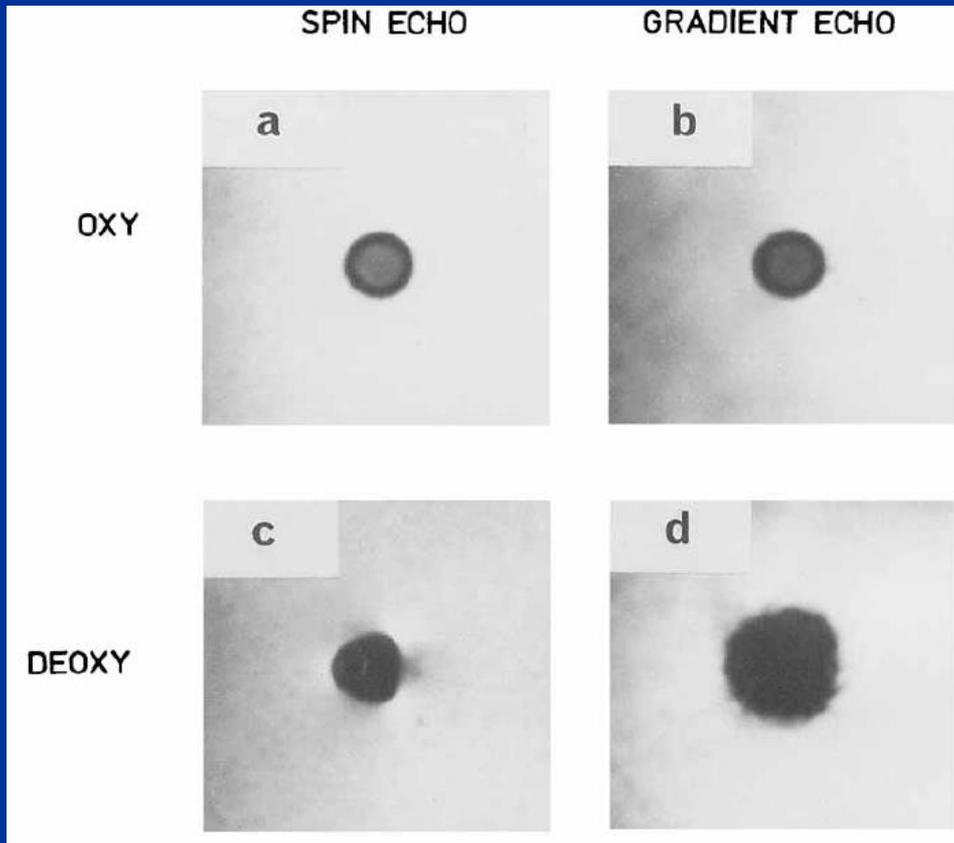
90%



Uniform Field



BOLD Signal Changes



Ogawa, S., Lee, T. M., Nayak, A. S., & Glynn, P. (1990). Oxygenation-sensitive contrast in magnetic resonance image of rodent brain at high magnetic fields. *Magnetic Resonance in Medicine*, 14(1), 68-78.

T2* - T2 decay with Susceptibility Effects

- $R2'$ relates to susceptibility properties of blood:

$$R2' \approx \kappa\gamma\Delta BV$$

$$= \kappa\gamma B_0 \text{Hct}(1 - Y)\chi_{\text{deoxy}}V$$

- κ is a constant
 - ΔB is the distortion of the field induced by the blood
 - V is blood volume fraction
 - Observe that the BOLD decay rate is proportional to B_0
- As oxygenation (Y) goes down, the decay rate $R2'$ goes up (faster decay)

BOLD Changes

- Consider that the total amount of deoxyhemoglobin is:

$$Q = V \text{Hct} (1-Y)$$

- Thus

$$R2' = \kappa \gamma B_0 \chi_{\text{deoxy}} Q$$

- $R2^*$ changes are directly proportional to changes in total deoxyhemoglobin (in a voxel):

$$\Delta R2^* = \Delta R2' \propto \Delta Q$$

R2* and R2'

- Some have suggested, based on computer modeling a more nonlinear relationship with respect to blood O2:

$$R2' = \kappa\gamma B_0 \text{Hct} \chi_{\text{deoxy}} V (1 - Y)^\beta$$

- β is a constant that ranges from 1-2, typically assumed to be about 1.5
- We'll use this relationship later...

MRI Signal Changes with R2'

- Let the signal at the echo time be:

$$m = m_0 e^{-\frac{TE}{T2^*}} = m_0 e^{-TE \cdot R2^*}$$

$R2^*b$ – the baseline rate

$R2^*a$ – the activation relaxation rate

- Fractional (%) signal change:

$$\Delta\% = \frac{m_a - m_b}{m_b} = \frac{m_0 e^{-TE \cdot R2^*_a} - m_0 e^{-TE \cdot R2^*_b}}{m_0 e^{-TE \cdot R2^*_b}}$$

$$\begin{aligned}\Delta\% &= e^{-TE \cdot \Delta R2^*} - 1 \\ &\approx -TE \cdot \Delta R2'\end{aligned}$$

MRI Signal Changes with Deoxyhemoglobin

- Fractional (%) Signal Change:

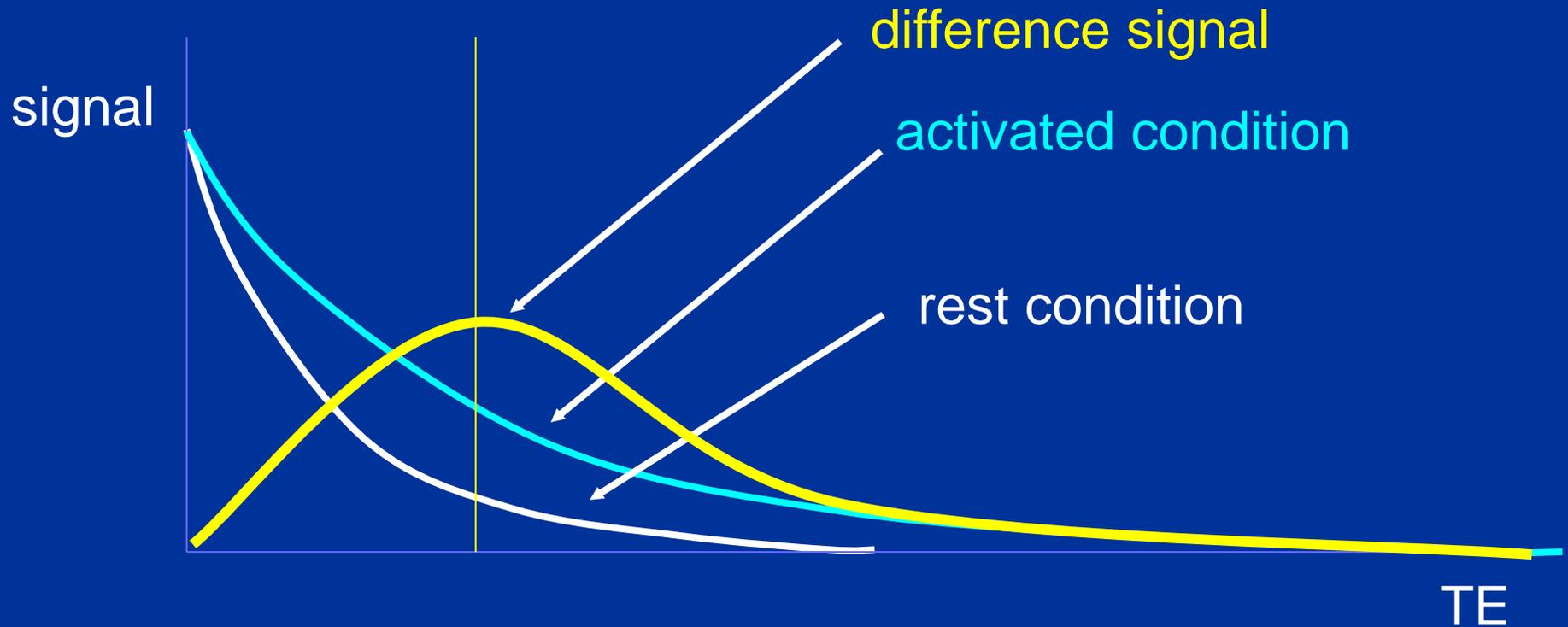
$$\Delta\% = \frac{m_a - m_b}{m_b} \approx -TE \cdot \Delta R2'$$

- But $\Delta R2^* = \Delta R2'$ is roughly proportional to change in total deoxyhemoglobin, so:

$$\% \text{ BOLD} \propto -\Delta Q$$

Optimization of TE

Maximum signal difference occurs at $TE \approx T2^*$



Problem – $T2^*$ varies across the head, but you have to pick 1 TE
(Note that we usually pick a TE that is shorter than the optimal.)

Relationship to Metabolism

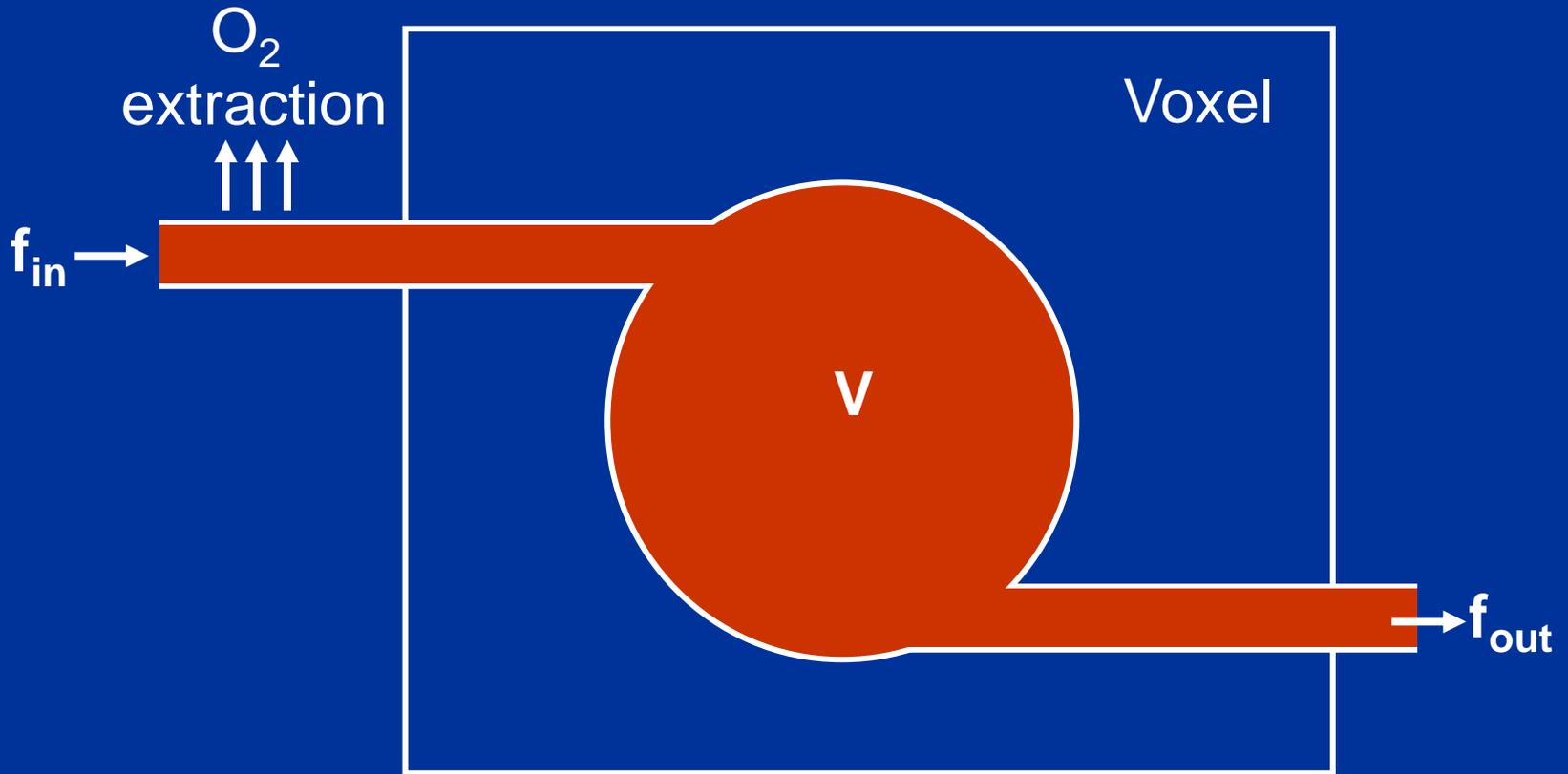
- Of interest is the relationship between the BOLD signal and oxygen metabolism

CMRO₂ = cerebral metabolic rate of O₂

$$\text{CMRO}_2 = C \cdot f \cdot \text{Hct} \cdot \text{OEF}$$

- f = perfusion rate (CBF) in ml/min/(100 g tissue)
 - OEF = oxygen extraction fraction
 - C = constant related to O₂ capacity of hemoglobin
- This expression says “amount consumed is equal to amount delivered”
 - Known as Fick’s Principle

Tissue Compartment Model



Assuming that most of the fMRI signal comes from the venous side, then:

$$OEF = 1 - Y$$

Fick's Principle

- We can now solve for some constants:

$$\frac{\text{CMRO2}}{f(1-Y)} = C \cdot \text{Hct}$$

- And equate these constants for baseline and activation states:

$$\frac{\text{CMRO2}_a}{f_a(1-Y_a)} = \frac{\text{CMRO2}_b}{f_b(1-Y_b)}$$

or

$$\frac{(1-Y_a)}{(1-Y_b)} = \frac{f_b}{f_a} \frac{\text{CMRO2}_a}{\text{CMRO2}_b}$$

Connection to BOLD

- Recall that that fractional signal change is:

$$\frac{m_a - m_b}{m_b} \propto \Delta \left[V(1-Y)^\beta \right] \propto V_b(1-Y_b)^\beta - V_a(1-Y_a)^\beta$$

- Rearranging, we get:

$$\frac{m_a - m_b}{m_b} = M \left[1 - \frac{V_a}{V_b} \left(\frac{1-Y_a}{1-Y_b} \right)^\beta \right]$$

where M is a constant (includes baseline properties)

The BOLD/CMRO2/CBF Connection

- Combining the above expressions we get:

$$\frac{m_a - m_b}{m_b} = M \left[1 - \frac{V_a}{V_b} \left(\frac{f_b}{f_a} \frac{\text{CMRO2}_a}{\text{CMRO2}_b} \right)^\beta \right]$$

The CBF/CBV Connection

- We can also assume a volume flow relationship:

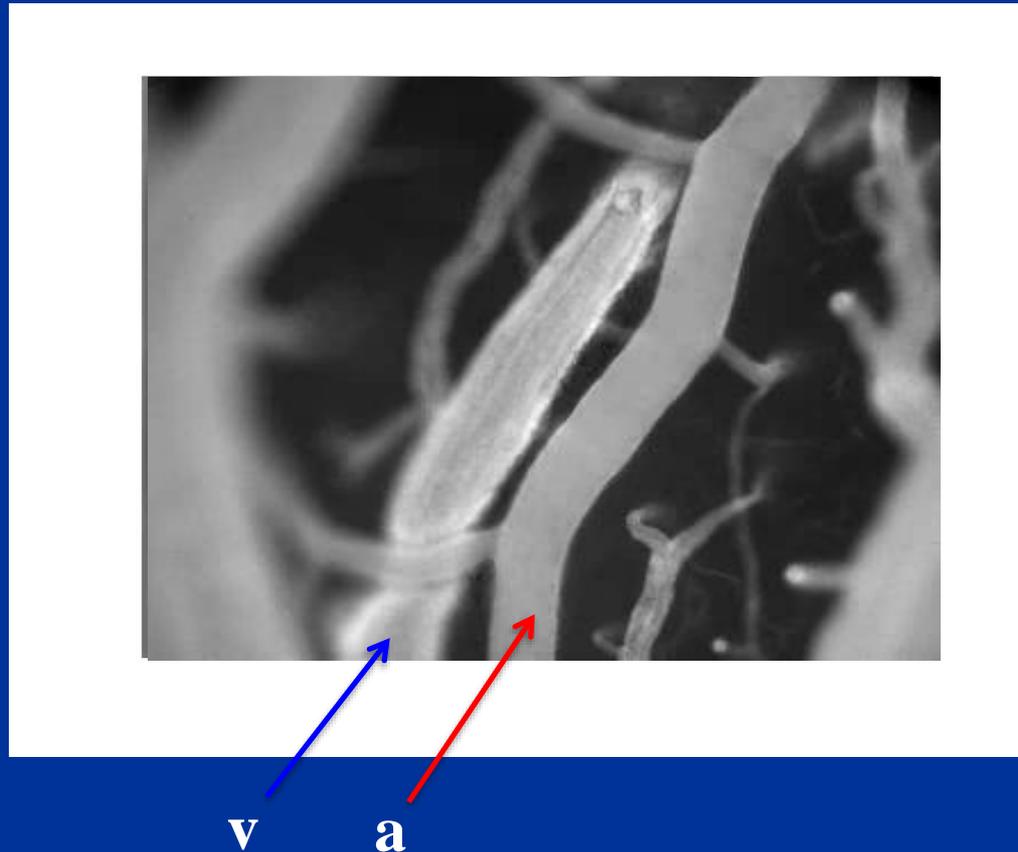
$$\frac{V_a}{V_b} = \left(\frac{f_a}{f_b} \right)^\alpha$$

Grubb's Relationship ($\alpha = 0.38$)

- Warning – this is problematic because most volume changes are on the arterial side and most deoxy-Hb changes are on the venous side. Nevertheless, we will use it 😊.

Volume Changes

- Mostly on the arterial side



The BOLD/CMRO2/CBF Connection

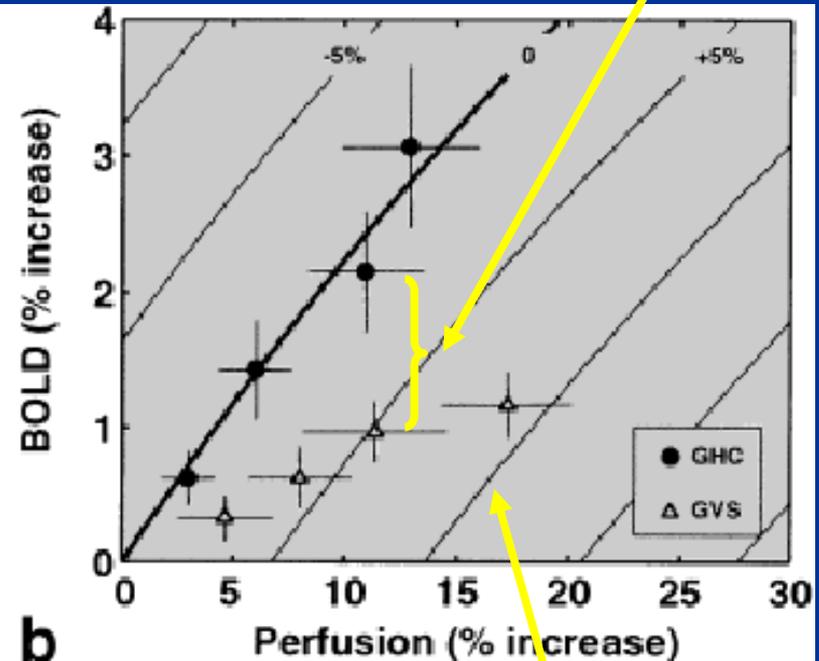
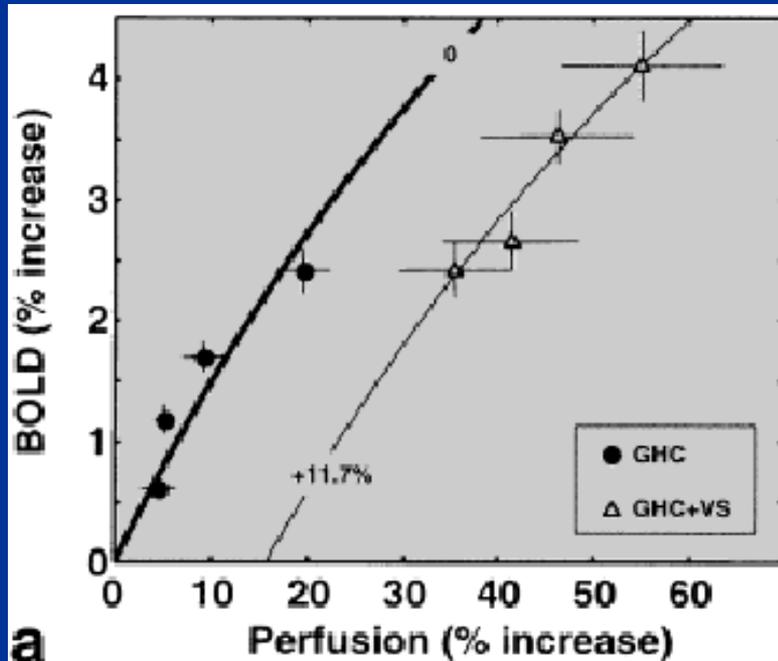
- Finally, we get:

$$\frac{m_a - m_b}{m_b} = M \left[1 - \left(\frac{f_b}{f_a} \right)^{\beta - \alpha} \left(\frac{\text{CMRO2}_a}{\text{CMRO2}_b} \right)^{\beta} \right]$$

- Observations:
 - As flow increases, BOLD increases
 - As CMRO2 increases, BOLD decreases

The BOLD/CMRO2/CBF Connection

This difference due to CMRO2



GHC = Graded Hypercapnia
GVS = Graded Visual Stimulation

Lines of constant CMRO2

(Hoge RD, et al. Magn. Reson. Med. 1999; 42:849-863.)

Can CMRO2 Ratios Be Determined?

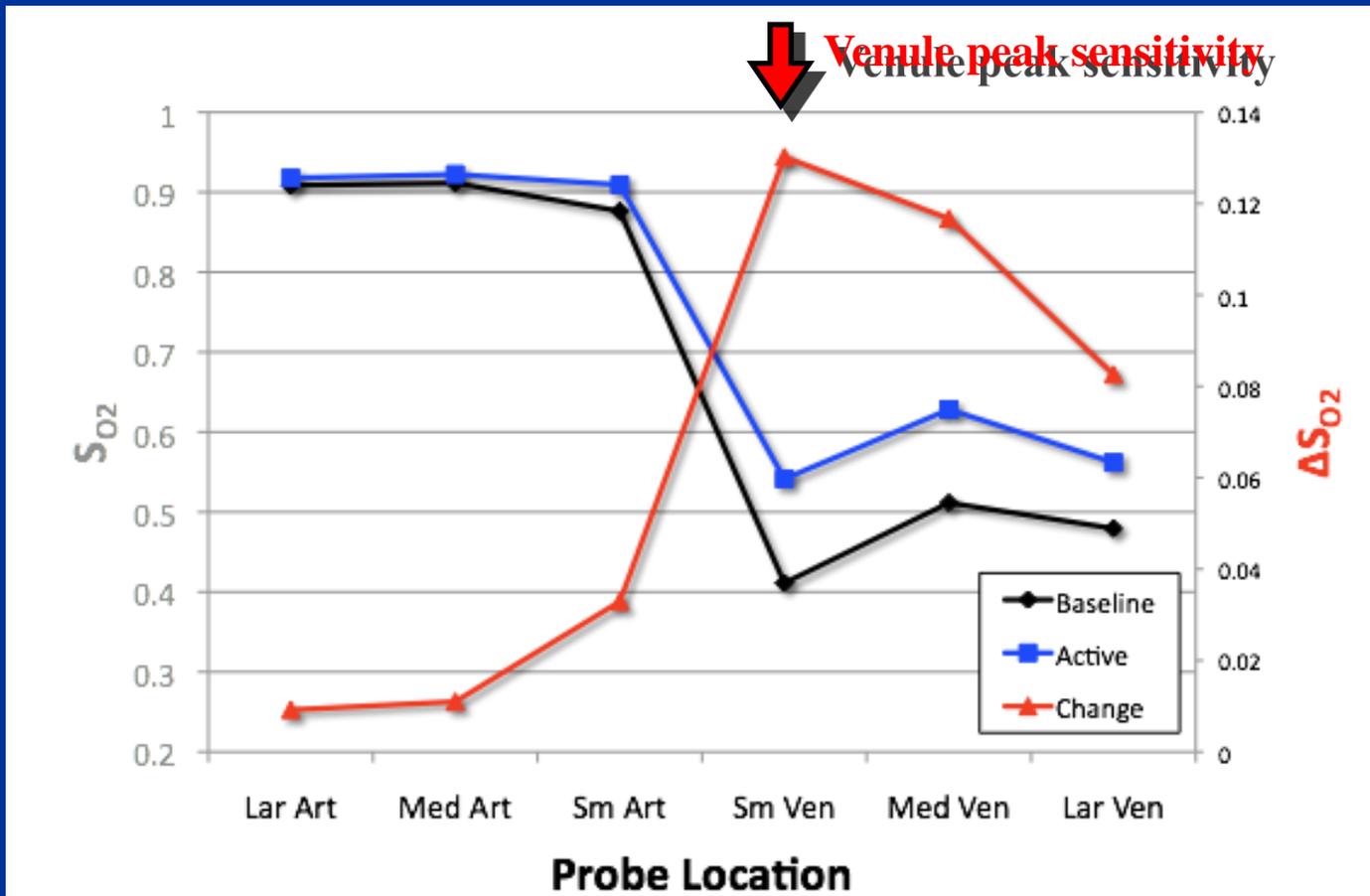
- Maybe...

$$\frac{m_a - m_b}{m_b} = M \left[1 - \frac{V_a}{V_b} \left(\frac{f_b}{f_a} \frac{\text{CMRO2}_a}{\text{CMRO2}_b} \right)^\beta \right]$$

- Need BOLD fractional signal change
- Need CBF measurements (f_a/f_b)
- Need volumes or assume Grubb's relationship
- Need constant M
(This can be done making the above measurements in a hypercapnia challenge – no CMRO2 changes!)

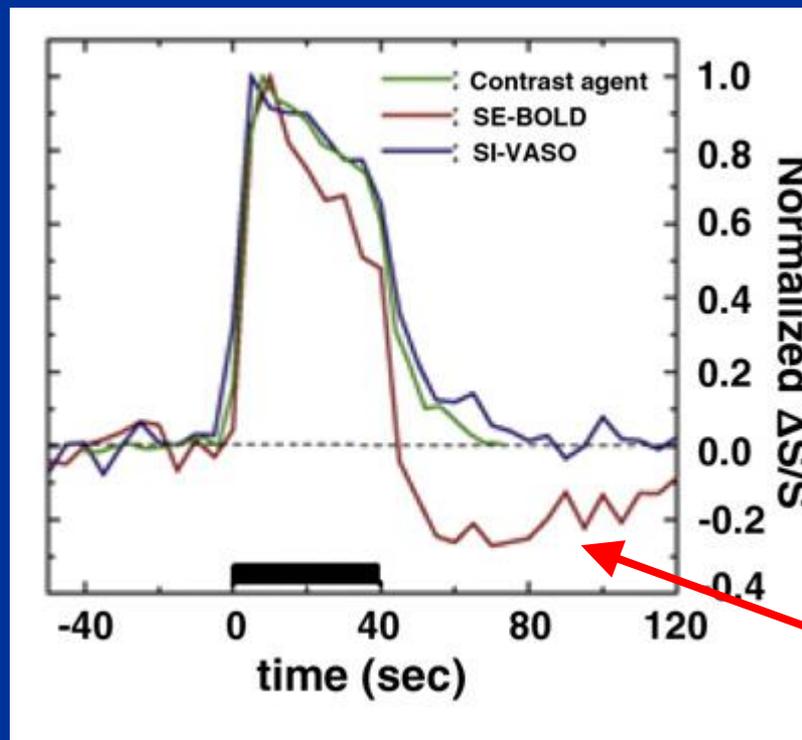
Complicating Factors...

O2 Saturation by Vessel Size



Post-Stimulus Undershoot

- One interesting feature of the fMRI response is the “post-stimulus undershoot”

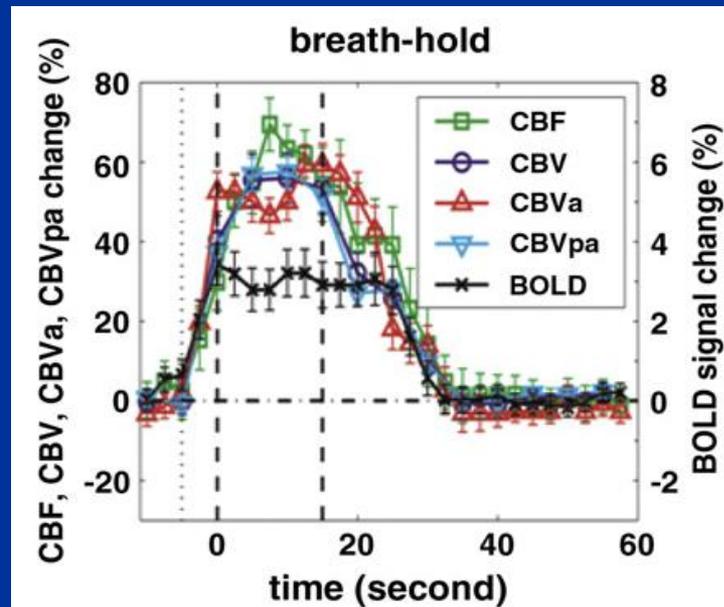
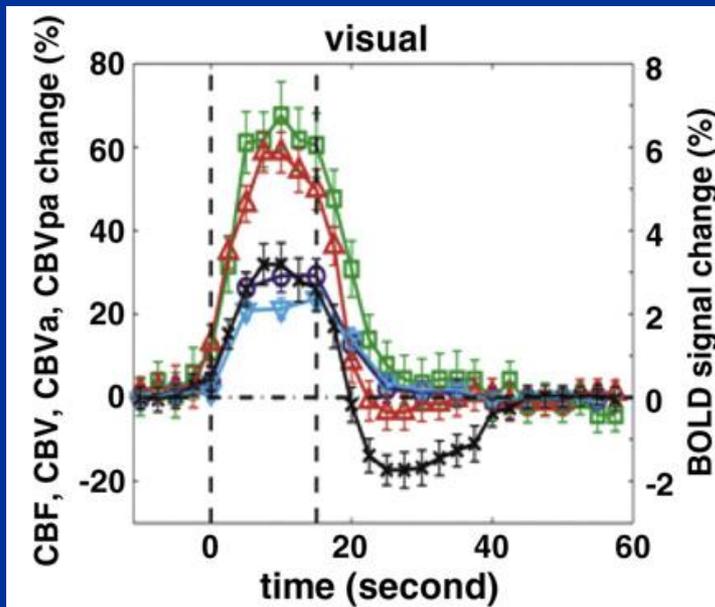


BOLD
undershoot

Post-Stimulus Undershoot

- Most likely sources
 - Persistent elevation of (venous) volume
 - Persistent elevation of CMRO₂

van Zijl, Hua, Lu.
NeuroImage 62 (2012)
1092–1102



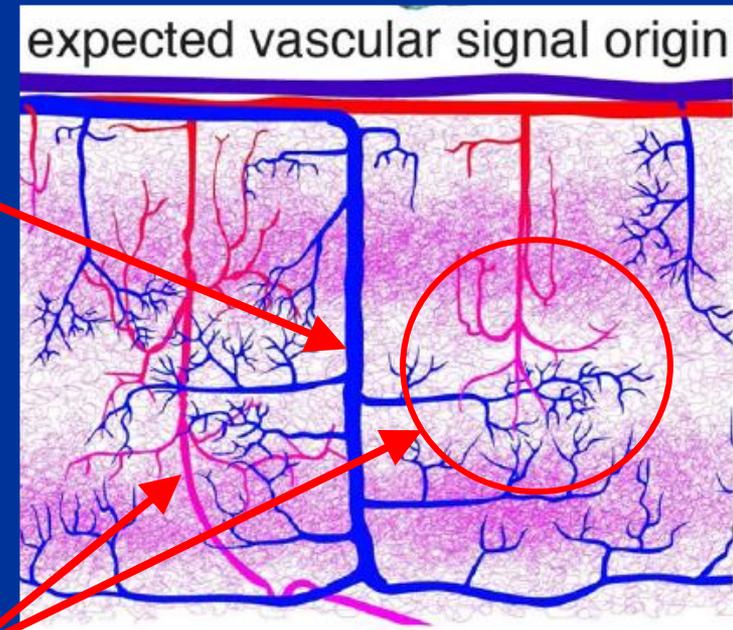
- These data suggest continued CMRO₂ is the dominant source

Outline

- Mechanism of the BOLD response
- Spatial specificity of BOLD and alternatives
- Evidence for and mechanisms of non-linearity
- Implications for fMRI Studies
- Conclusions

Spatial Specificity

- BOLD vs. other mechanisms
 - Since BOLD is venous weighted, it has substantial signals along the cortical surface
- Perfusion and Volume changes are mostly deeper
 - Perfusion – capillaries
 - CBV – arterioles



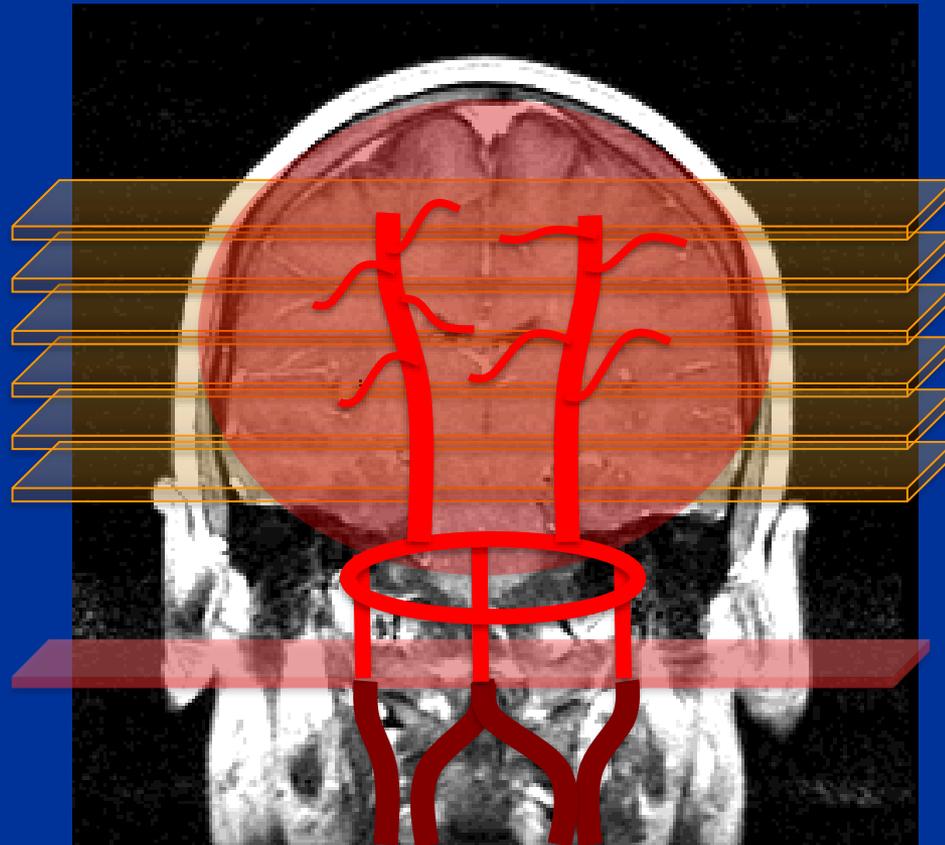
Huber L, et al. Progress in Neurobiology, 2020.

CBF and CBV Methods

- Cerebral Blood Flow (CBF) with MRI
 - Most common is Arterial Spin Labeling (ASL) with the most common version of that being:
 - pCASL (pseudo-continuous ASL)
 - Works well, but low SNR and slower than BOLD
- Cerebral Blood Volume (CBV) with MRI
 - Contrast agent methods
 - Increasingly popular – Vascular Space Occupancy (VASO) methods
 - Also works well, but hard to get large volumes and lower SNR than BOLD

Continuous ASL (CBF)

1. Detre JA, Leigh JS, Williams DS, Koretsky AP. **Perfusion imaging.** *Magn. Reson. Med.* 1992; 23:37–45.
2. Dai W, Garcia D, De Bazelaire C, Alsop DC. **Continuous flow-driven inversion for arterial spin labeling using pulsed radio frequency and gradient fields.** *Magn. Reson. Med.* 2008;60:1488–1497.



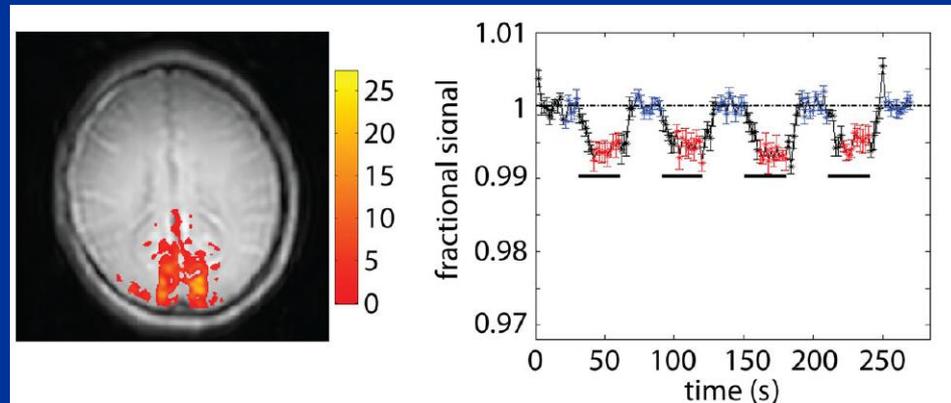
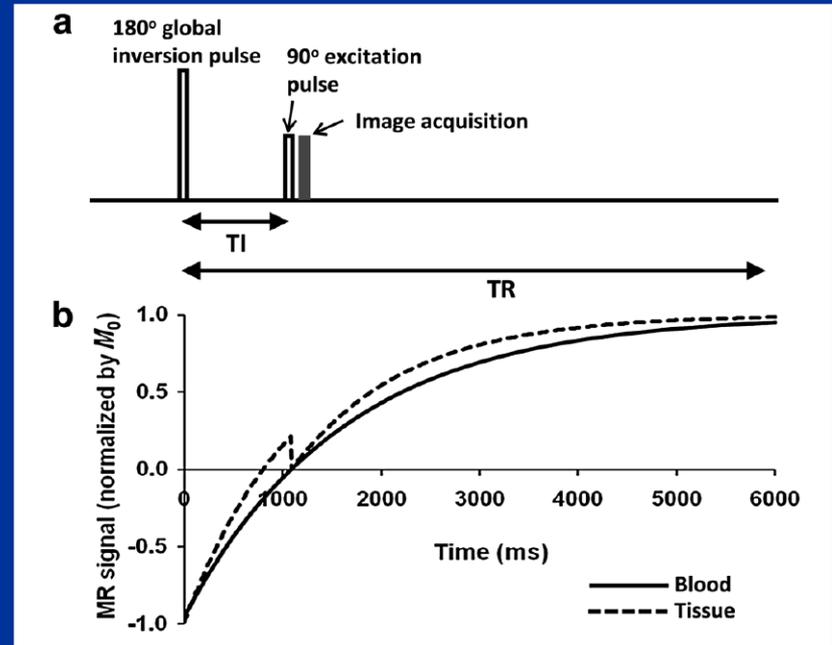
ASL Acquisition.
Hernandez-Garcia, 2019

CBV Methods (e.g. VASO)

- VASO inverts the entire volume and images where the blood is nulled out
- Signal decreases as blood volume increases

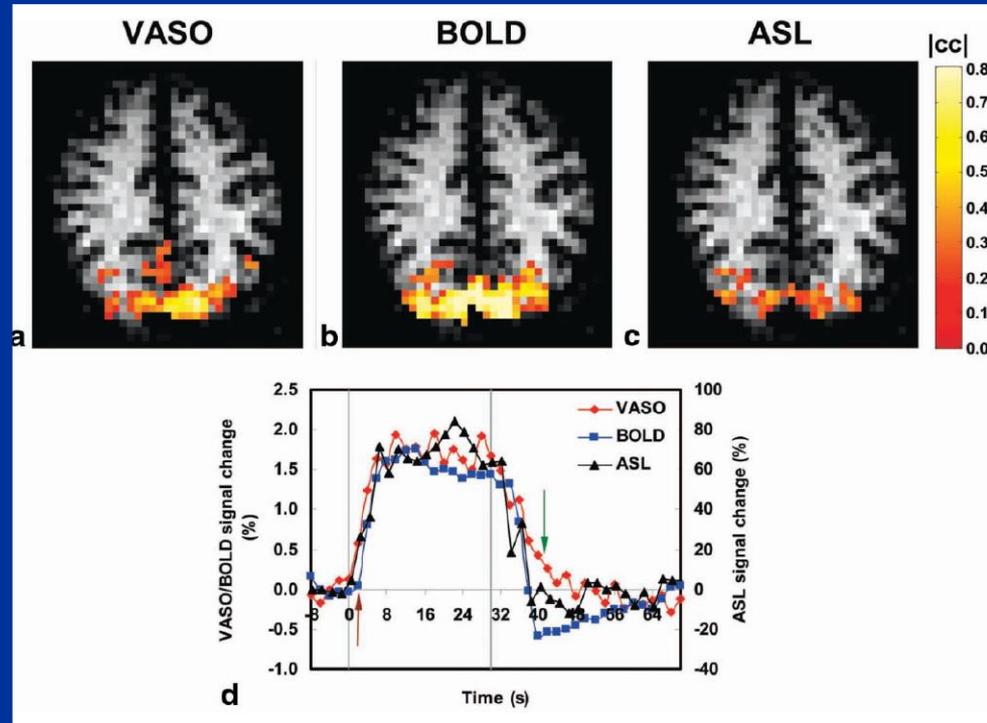
VASO: Lu, H., Hua, J., & van Zijl, P. C. (2013). Noninvasive functional imaging of cerebral blood volume with vascular-space-occupancy (VASO) MRI. *NMR in Biomedicine*, 26(8), 932-948.

Other methods, e.g. Jahanian, H., Peltier, S., Noll, D. C., & Hernandez Garcia, L. (2015). Arterial cerebral blood volume-weighted functional MRI using pseudocontinuous arterial spin tagging (AVAST). *Magnetic resonance in medicine*, 73(3), 1053-1064.



VASO/ALS vs. BOLD

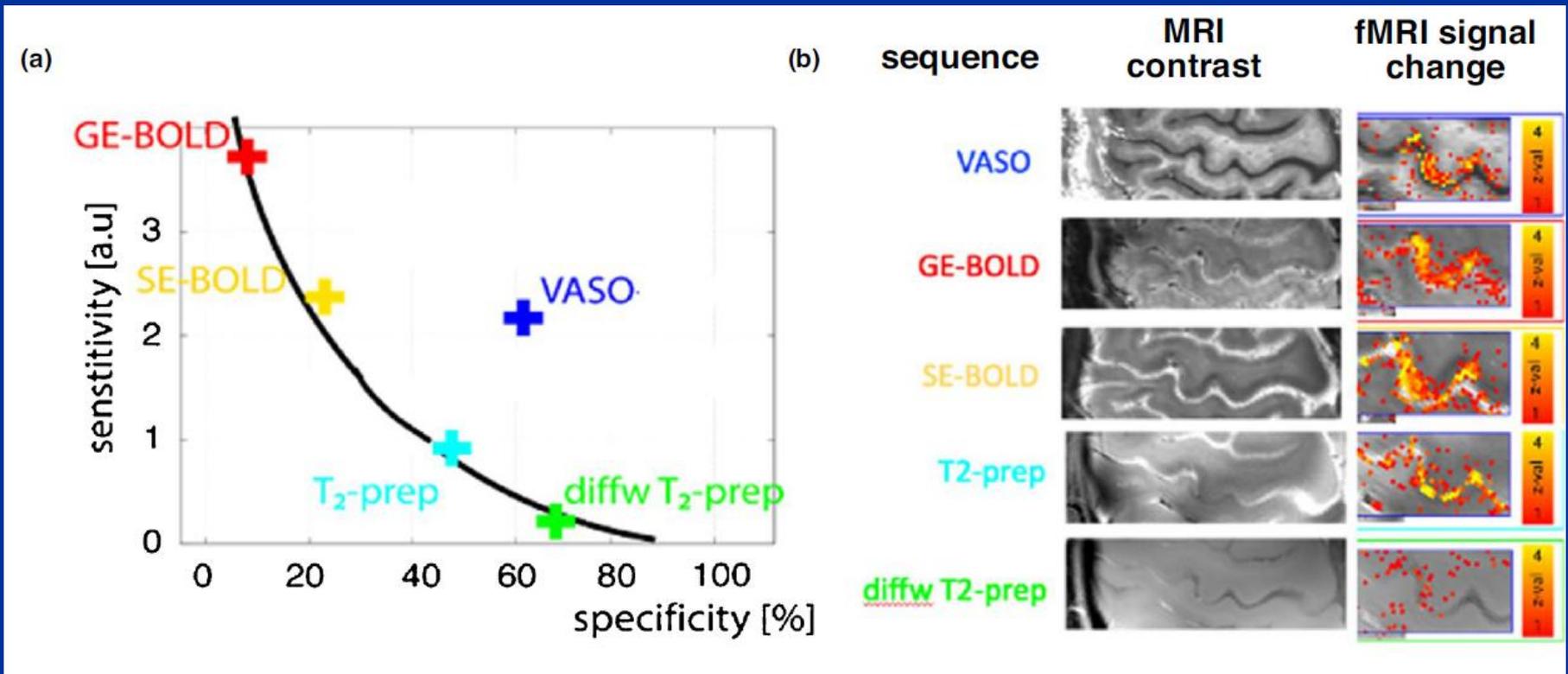
- ASL – spin exchange focused on capillaries
- VASO – signals focused where volume changes most
- BOLD – signals where blood oxygenation changes



Lu H, et al. MRM, 50:263–274 2003.

Vascular Specificity vs. SNR

Note that these images are 7T MRI – not everything is the same at 3T



VASO/ALS vs. BOLD

- VASO is often pitched for high-resolution, layer- or column-specific fMRI
 - Requires small voxels and is more appropriate for 7T MRI (though there is a little bit of work at 3T)
- SNR (sensitivity) and speed issues have limited the interest in VASO and ALS at 3T
- Still, it may be of interest if subtle localization changes (e.g. topographic mapping) is important

Outline

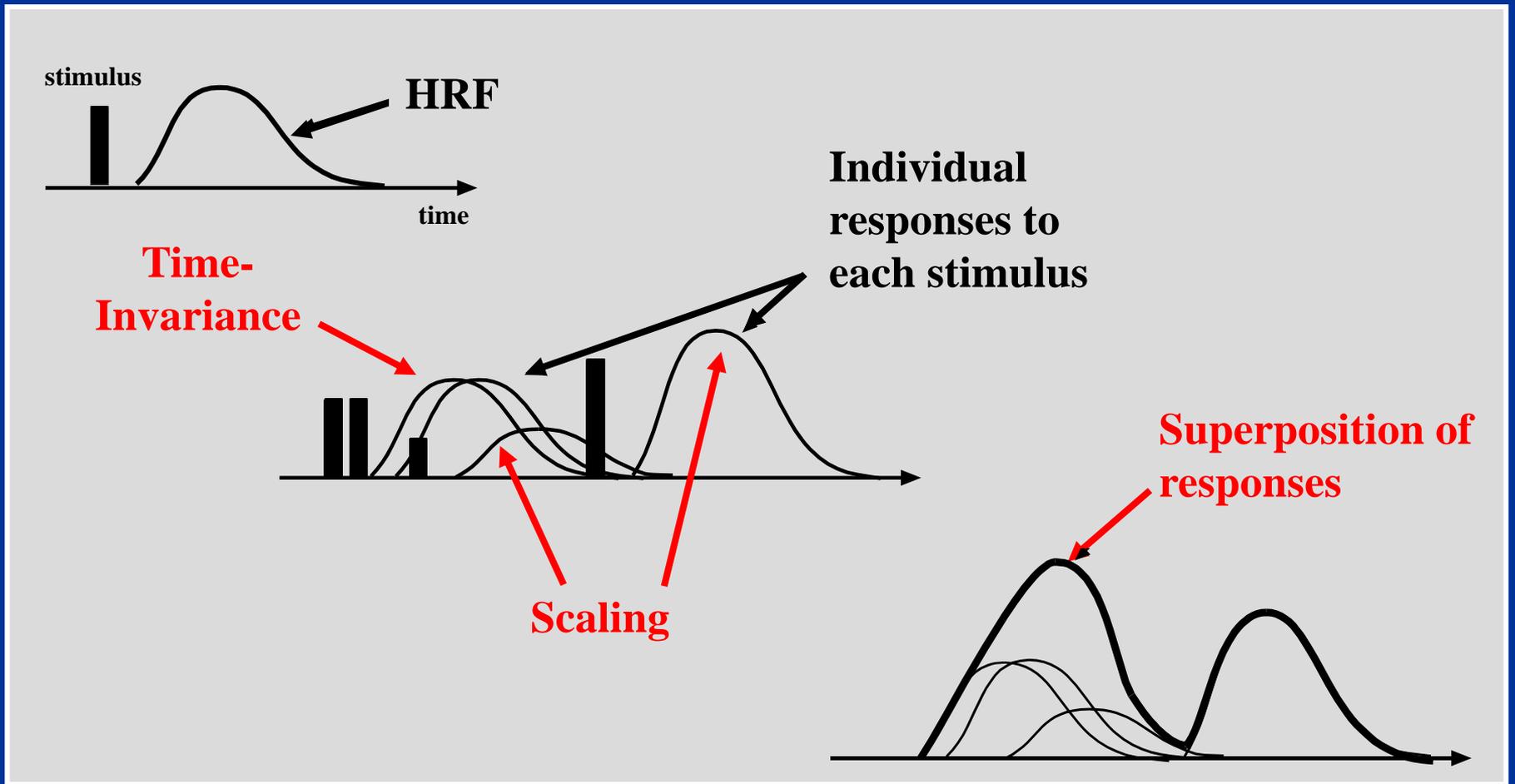
- Mechanism of the BOLD response
- Spatial specificity of BOLD and alternatives
- Evidence for and mechanisms of non-linearity
- Implications for fMRI Studies
- Conclusions

Linearity

A “linear system” satisfies the following:

- Scaling
 - Increasing stimulation by some ratio will increase the output by the same ratio
- Superposition (additivity)
 - Combining (adding) any two stimuli will lead to an output that is the sum of the two responses
- Time-invariance
 - A response is the same irrespective of when it comes or what precedes or follows it

Superposition and Predicted Responses



Why Is Linearity Good?

- Extensive theory of linear systems
- Allows definition of an “impulse response function”
 - Commonly known as the hemodynamic response function (HRF)
- Predicted responses are easily determined
 - Can also allow “deconvolution” of response to get estimates of the system input

Is the BOLD response linear?

- In many cases, it is almost linear.
- In other cases, it is not very linear, notably:
 - Manipulations of task (block) duration for short (less than 4 s) blocks
 - Repeated stimuli after long (e.g. 30 s) rest periods
 - Other effects

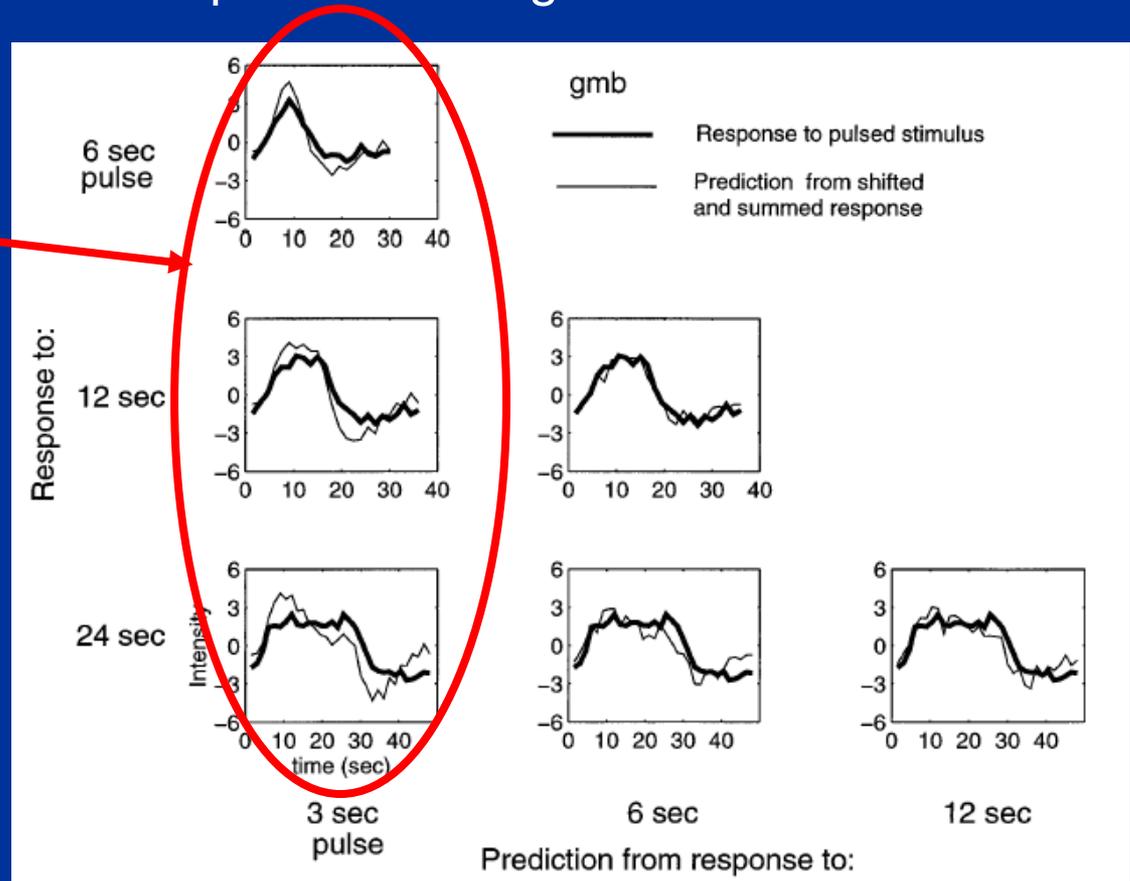
Manipulations in Task Duration

Linearity implies that responses from short stimuli should predict responses to longer stimuli

Response from 3 s stimulus poorly predicted responses to 6, 12 and 24 s stimuli.

But, response from 6 s stimulus was a good predictor.

→ The “system” behaves nonlinearly for 3 s stimuli.



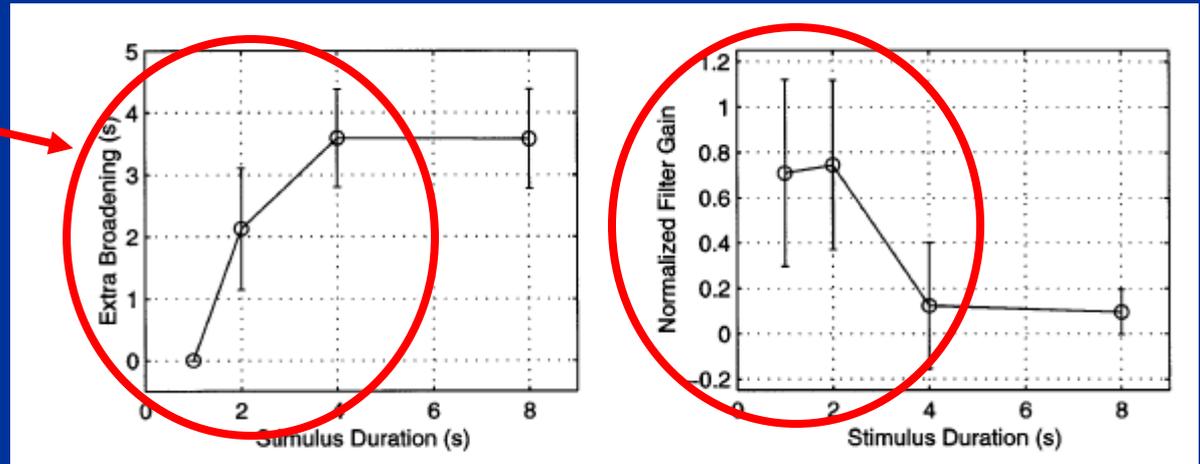
(Boynton GM, et al. J Neuroscience 1996; 16:4207-4221.)

Manipulations in Task Duration

A system model should remain the same regardless of stimulus duration

Estimated model parameters varied for short stimuli.

→ The “system” produced shorter and more intense responses for stimuli less than 4 s in duration.



(Vazquez AL, Noll DC. NeuroImage 1998; 7:108-118.)

- The same study also showed some nonlinearities with manipulations in stimulus intensity.

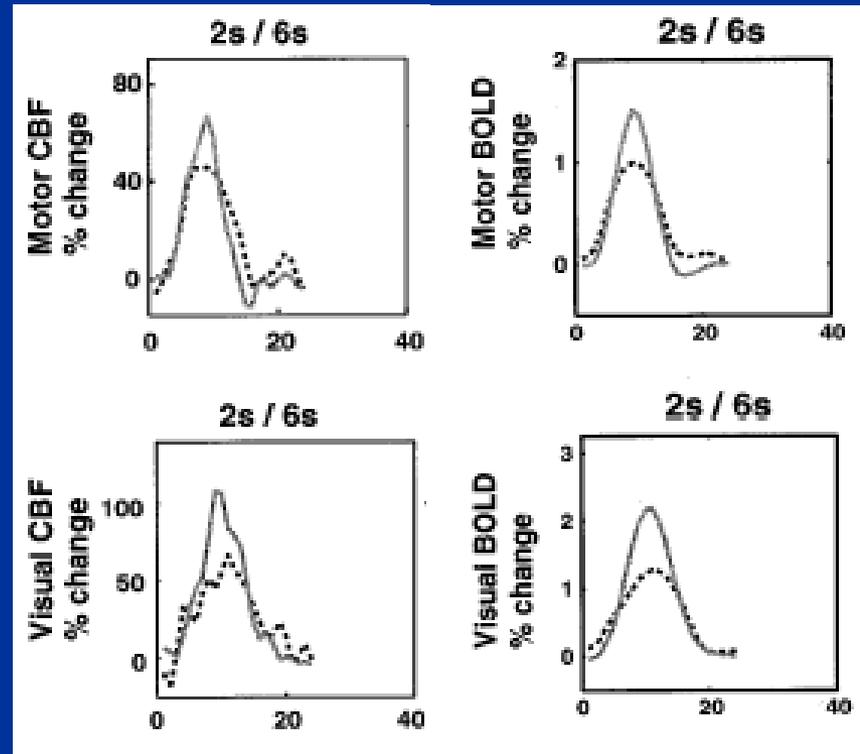
Nonlinearity in the CBF

Nonlinearity in predicting responses also appears cerebral blood flow (CBF) as well as BOLD

Response from 2 s stimulus poorly predicted responses to 6 stimulus for .



→ Nonlinearities occur broadly in the vascular response.



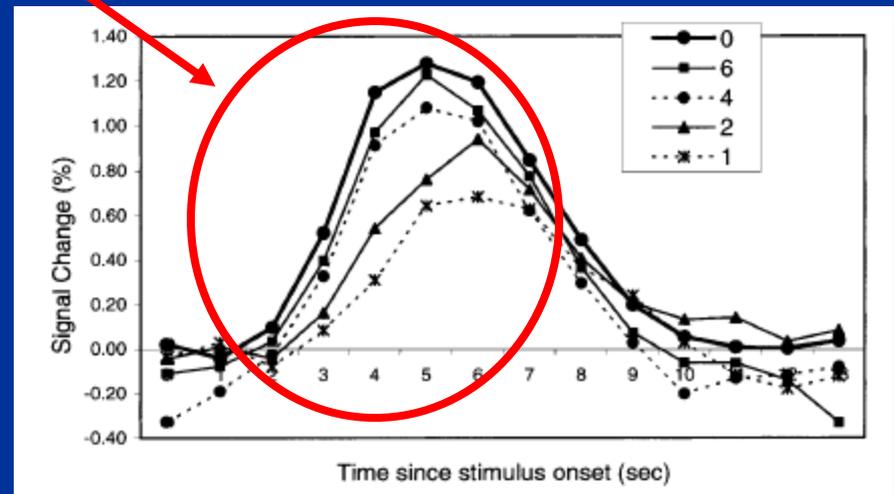
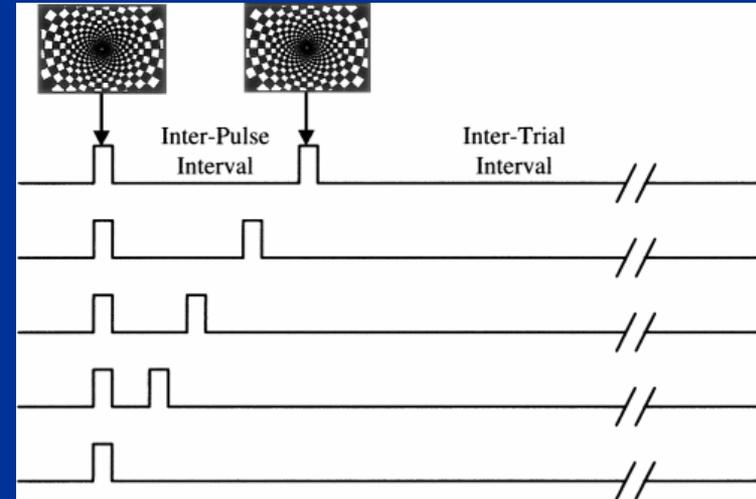
(Miller KL, et al. Human Brain Mapping 2001; 13(1):1-12.)

Responses to Repeated Stimuli

Explicit manipulation of inter-stimulus interval demonstrates that subsequent responses are delayed and less intense.

→ The “system” response is time-variant and the degree depends on time to preceding stimulus.

→ Long latencies (as much as 1 s) imply that some effects are not neural in origin.



(Huettel SA, McCarthy G. Neuroimage 2000; 11:547-553.)

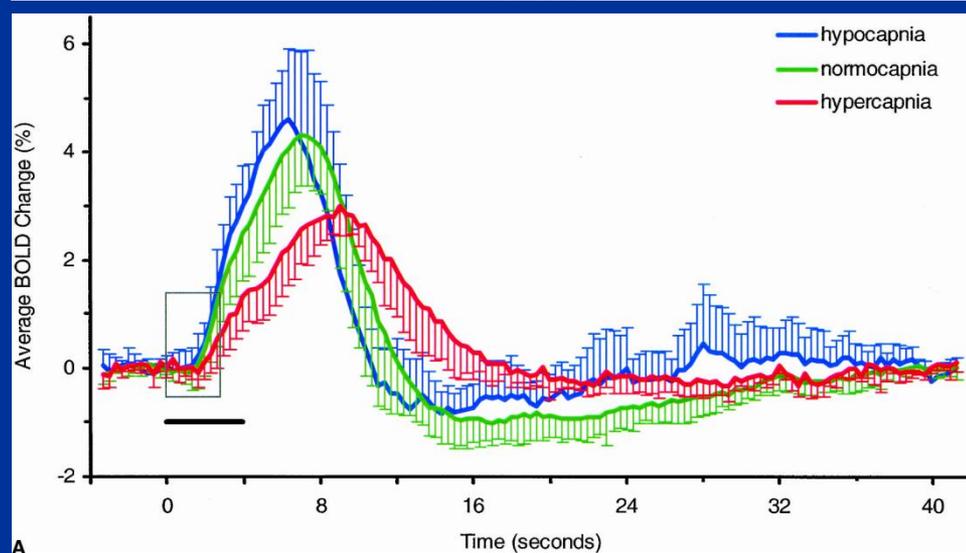
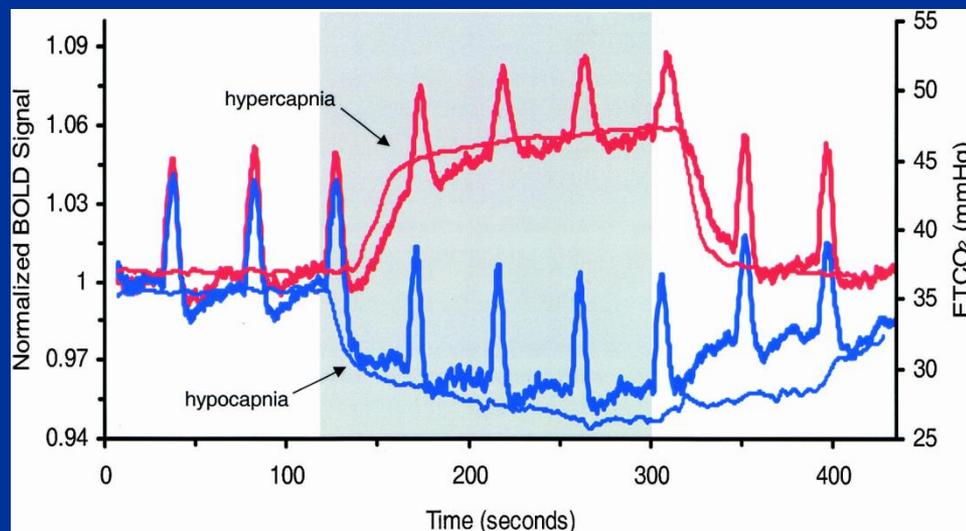
Mechanisms for Nonlinear Behavior

- Vascular
 - Non-linear (e.g. visco-elastic) behavior of vessels
 - Non-linear coupling/control of vascular response
 - Non-linear extraction of oxygen from blood pool
- Neural
 - Non-linear neural response to stimulus or task (e.g. novelty, threshold effects)
 - Synaptic activity (including inhibitory) vs. firing rate
- Metabolic
 - Non-linear relationship between metabolism and neural activity

(Not meant to be an exhaustive list.)

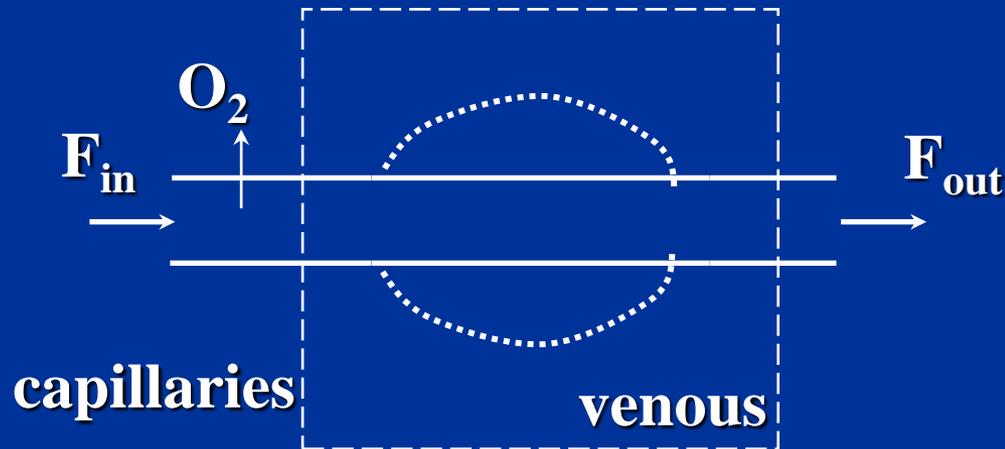
Vascular Mechanisms for Nonlinearity

- Manipulations in basal flow conditions through **hypercapnia** and **hypocapnia**
- Increased basal CBF leads to
 - Decreased intensity
 - Increased response width and latency
 - And vice-versa.
- **Basal flow conditions affect BOLD response**



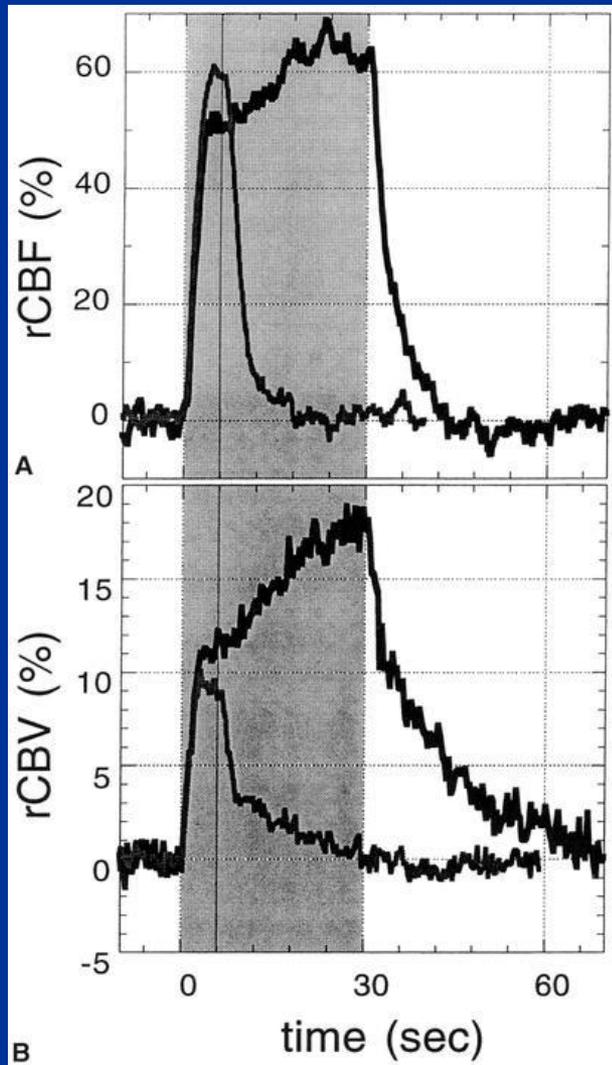
(Cohen, et al., *JCBFM* 2002; 22:1042-1053.)

Vascular Mechanisms for Nonlinearity



- The “balloon” model (Buxton RB, et al. Magn Reson Med 1998; 39:855-864) can predict some of the observed nonlinearities.
- This model can explain the persistent elevation of cerebral blood volume (CBV), perhaps through visco-elastic behavior.

Vascular Mechanisms for Nonlinearity

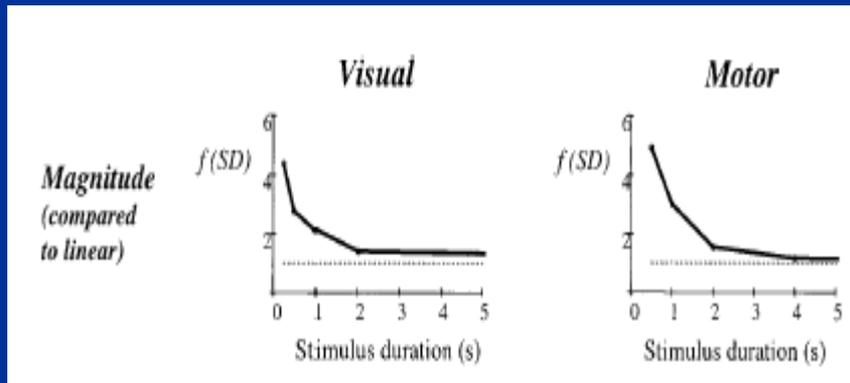


- Cerebral blood volume (CBV) response returns to baseline more slowly than the CBV onset
- Elevated CBV effectively changes the basal physiological conditions
- Could cause time-variant behavior

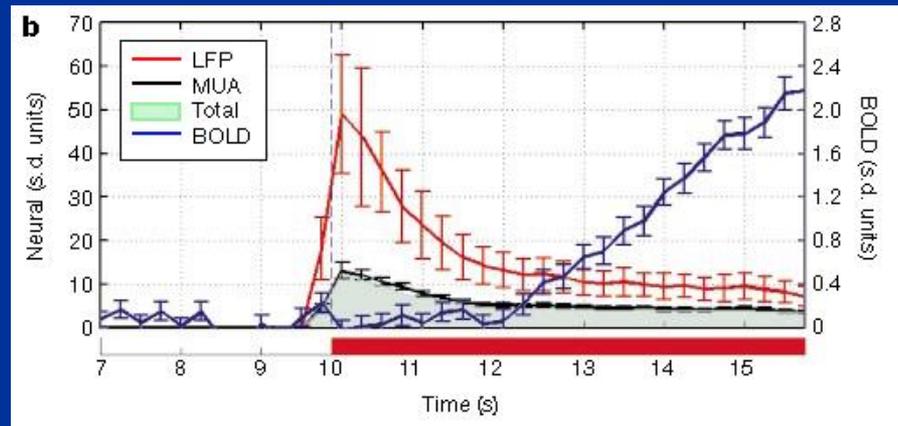
(Mandeville JB, et al. *JCBFM* 1999; 19:679-689.)

Neural Mechanisms for Nonlinearity

- Neural networks are nonlinear.
- Some observed nonlinearities could be caused by neural mechanisms, for example:
 - Changes in apparent BOLD magnitude response with stimulus duration are similar to measured in local field potentials (LFP's).
 - BOLD response found to be closely correlated with LFP's.



(Birn RM, et al. Neuroimage 2001; 14(4):817-826.)



(Logothetis NK, et al. Nature 2001; 412(6843):150-157)

Metabolic Mechanisms for Nonlinearity

- There have been suggestions that oxygen metabolism may persist in a nonlinear fashion following activation
 - Alternate explanation of the post-stimulus undershoot of the BOLD response

Mechanisms for Nonlinear Behavior

- BOLD nonlinearity is a likely result of:
 - A combination of vascular and neural effects
 - Other mechanisms including metabolic rates and the coupling between neural activity and physiological responses.
- The good news is that we can deal many of these effects.

Outline

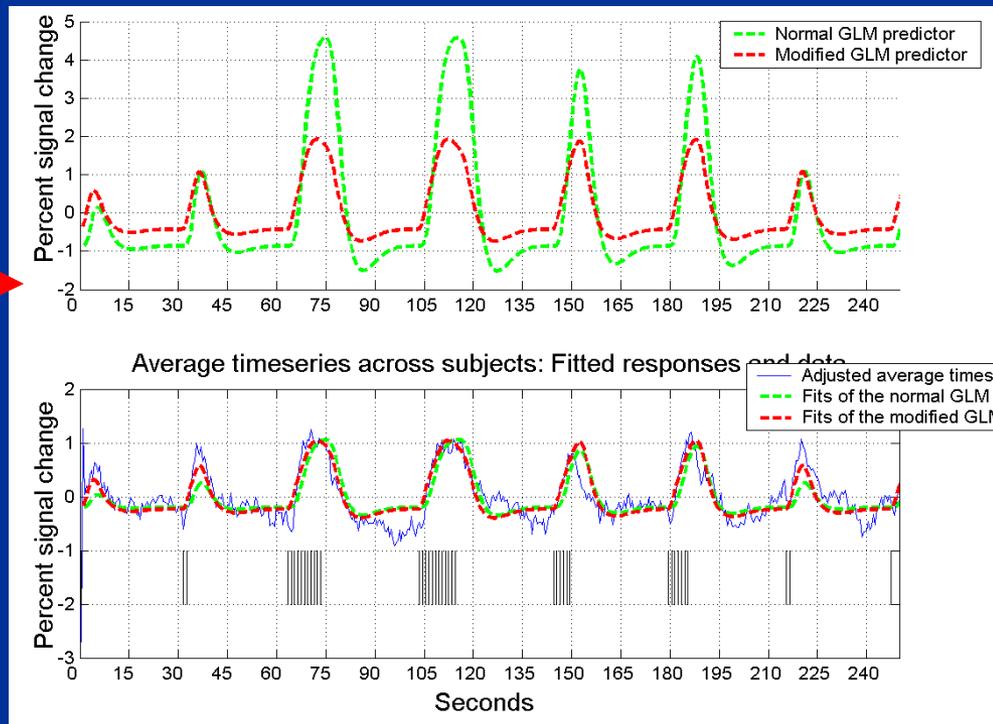
- Mechanism of the BOLD response
- Spatial specificity of BOLD and alternatives
- Evidence for and mechanisms of non-linearity
- Implications for fMRI Studies
- Conclusions

Avoiding Nonlinearities

- Blocked task designs
 - Long blocks do not exhibit much nonlinearity and are relatively immune to changes in shape of HRF
- Event-related task designs
 - Avoid combinations of long (> 30 s) and short (< 10 s) intertrial intervals
 - Rapid, random stimulus presentations give mostly linear response
 - No opportunity to return to basal neural or vascular conditions

Explicit Modeling of Nonlinearities

- One can also explicitly model the nonlinear effects and incorporate that into the development of reference functions for GLM analysis
- One can also explicitly model the nonlinearity through:
 - Use of Volterra kernels (Friston KJ, et al. Neuroimage 2000; 12(4):466-477)
 - Use of physiologically relevant models (Vazquez AL, et al., Human Brain Mapping 2003, New York and Feng CM, et al. NMR Biomed. 2001;14:397–401)
 - Many other approaches



(Wager, Vazquez, Hernandez, Noll, Neuroimage. 2005 Mar;25(1):206-18.)

Conclusions

- The temporal character of the BOLD response:
 - Results from complex chain of physiological events
 - Is fairly slow (time constants ≥ 5 s)
 - Exhibits some nonlinear characteristics
- BOLD is biased towards draining veins
 - Alternatives (CBF, CBV) are costly (SNR, speed)
- Linearity is important for accuracy in analysis and temporal feature extraction
 - Nonlinearity is likely caused by several mechanisms and is currently topic of ongoing research